

Marie Curie **RISE** Action

FunFiCO

(Fundamental Fields and Compact Objects)

Meeting at UNAM, Cuernavaca Campus, Mexico

April 16th 2018



# Marie Curie **RISE** Actions within Horizon2020 (**R**esearch and **I**nnovation **S**taff **E**xchange)

4 years project (Dec 2017 - Nov 2021)  
Fundamental Fields and Compact Objects (FunFiCO)

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# Testing the Kerr hypothesis

C. Herdeiro

Departamento de Física da Universidade de Aveiro, Portugal



*Gravitational lensing of the Aveiro Campus by a Kerr black hole with scalar hair*

Marie Curie RISE Action FunFiCO Meeting

Cuernavaca, Mexico,  
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# The Kerr hypothesis

“In my entire scientific life, extending over forty-five years, the most shattering experience has been the realization that an exact solution of Einstein’s field equations of general relativity, discovered by the New Zealand mathematician, Roy Kerr, provides the absolutely exact representation of untold numbers of massive black holes that populate the Universe.”

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1) are these untold numbers of massive black holes exactly represented by the Kerr metric ?

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- 1) are these untold numbers of massive black holes exactly represented by the Kerr metric ?
- 2) are these black holes all of the same type ?
- 3) are these objects really black holes ?

## Plan:

- 1) The Kerr model (uniqueness and no-hair theorems)
- 2) Black holes beyond Kerr (Non-Kerr/hairy BHs)
  - a) In General Relativity
  - b) Beyond General Relativity
- 3) Beyond black holes: Exotic Compact Objects Pedro Cunha's talk
- 4) Outlook

# **1) The Kerr Model**

# 1967-...: The electro-vacuum uniqueness theorems

## Axisymmetric Black Hole Has Only Two Degrees of Freedom

B. Carter

*Institute of Theoretical Astronomy, University of Cambridge, Cambridge CB3 0EZ, England*  
(Received 18 December 1970)

A theorem is described which establishes the claim that in a certain canonical sense the Kerr metrics represent “the” (rather than merely “some possible”) exterior fields of black holes with the corresponding mass and angular-momentum values.

Phys. Rev. Lett. 26 (1971) 331-333

Vacuum:

$$\mathcal{S} = \frac{1}{16\pi} \int d^4x \sqrt{-g} R$$

Kerr Kerr 1963

Uniqueness Israel 1967; Carter 1971;  
D.C. Robinson, Phys. Rev. Lett. 34, 905 (1975).

### Carter-Robinson theorem:

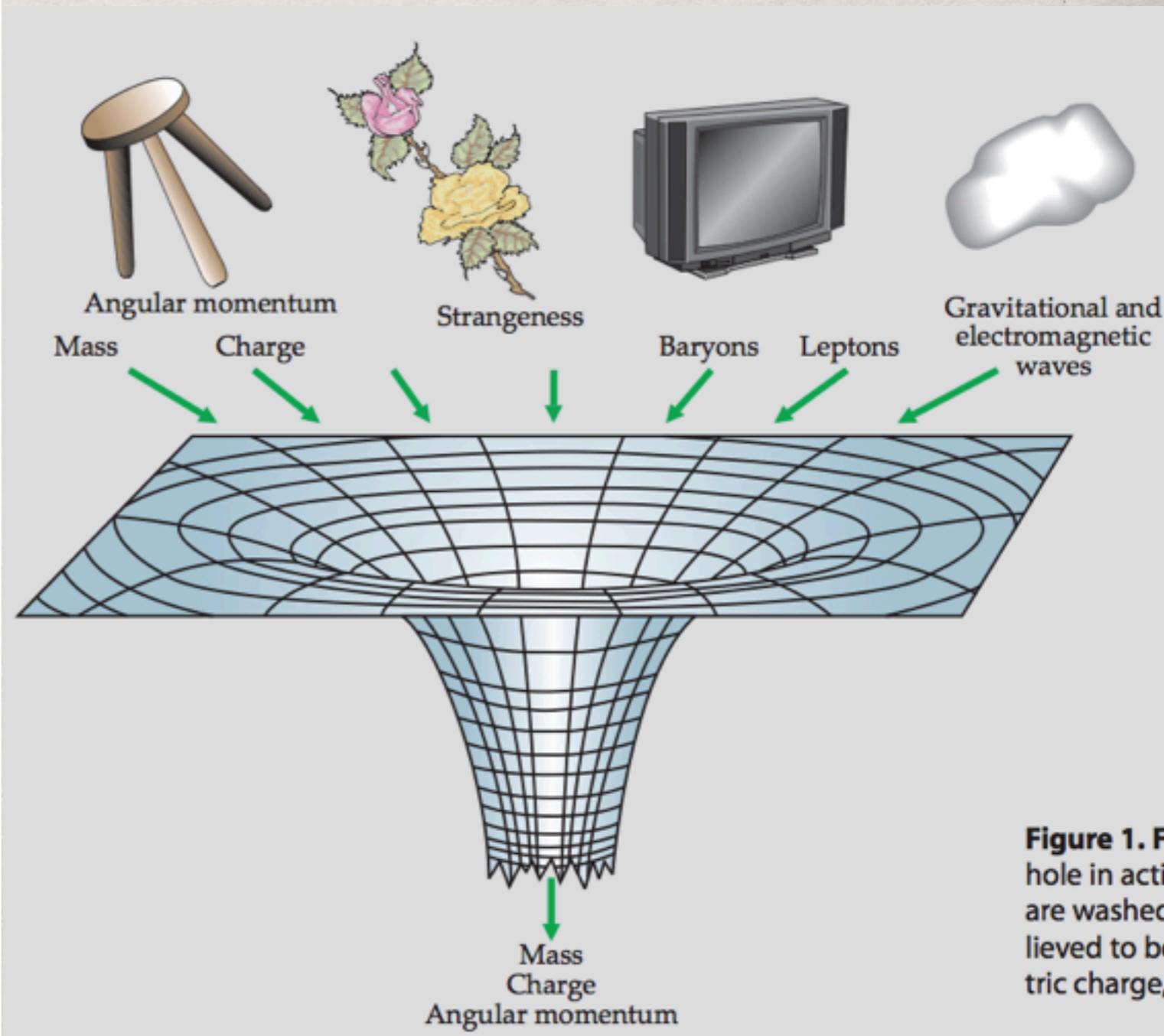
An asymptotically-flat stationary and axi-symmetric vacuum spacetime that is non-singular on and outside an event horizon, is a member of the two-parameter Kerr family.

The assumption of axi-symmetry was subsequently shown to be unnecessary, i.e. for black holes, stationarity  $\Rightarrow$  axisymmetry (via the “rigidity theorem”, relating the teleologically defined “event horizon” to the local “Killing Horizon” Hawking 1972; I. Rácz and R. Wald, Class. Quant. Grav. 13 (1996) 539).

# 1971: Wheeler and Ruffini coin the expression “a black hole has no hair”

The collapse leads to a black hole endowed with mass and charge and angular momentum but, so far as we can now judge, no other adjustable parameters: “A black hole has no hair.” Make one black hole out of matter; another, of the same mass, angular momentum, and charge, out of antimatter. No one has ever been able to propose a workable way to tell which is which. Nor is any way known to distinguish either from a third black hole, formed by collapse of a much smaller amount of matter and then built up to the specified mass and angular momentum by firing in enough photons, or neutrinos, or gravitons. And on an equal footing is a fourth black hole, developed by collapse of a cloud of radiation altogether free from any “matter.”

Electric charge is a distinguishable quantity because it carries a long-range force (conservation of flux; Gauss’s law). Baryon number and strangeness carry no such long-range force. They have no Gauss’s law. It is true that no attempt to observe a change in baryon number has ever succeeded. Nor has anyone ever been able to give a convincing reason to expect a direct and spontaneous violation of the principle of conservation of baryon number. In gravitational collapse, however, that principle is not directly violated; it is transcended. It is transcended because in collapse one loses the possibility of measuring baryon number, and therefore this quantity can not be well defined for a collapsed object. Similarly, strangeness is no longer conserved.



**Figure 1.** F  
hole in acti  
are wash  
believed to b  
tric charge,

# The “no-hair” conjecture :

## **The “no-hair” original idea (1971):**

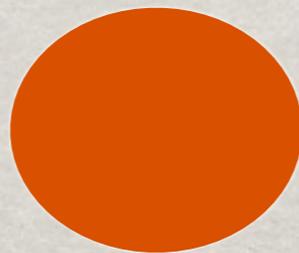
collapse leads to equilibrium black holes uniquely determined by  $M, J, Q$  - asymptotically measured quantities subject to a Gauss law and no other independent characteristics (hair)

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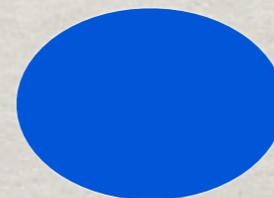
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The idea is motivated by the uniqueness theorems and indicates black holes are **very special objects**



Two stars  
with same  
 $M, J$



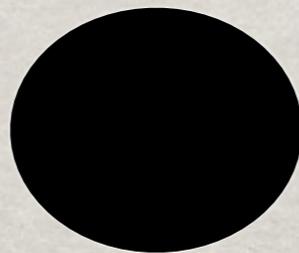
Can have a different mass quadrupole, etc...

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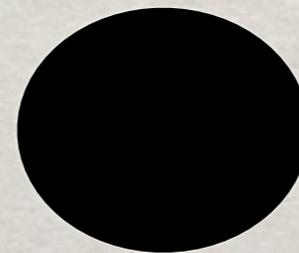
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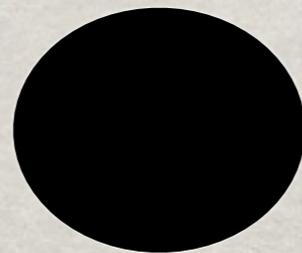
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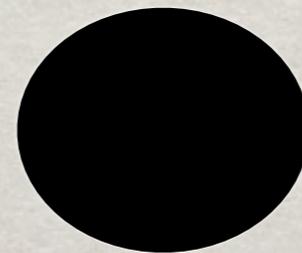
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...must be exactly equal...

Elegant multipoles formula  
(for the Kerr solution):

**R. O. Hansen,**  
**J. Math. Phys. 15 (1974) 46**

$$M_\ell + iS_\ell = M(ia)^\ell$$

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Three broad theoretical criteria for a good model of compact objects:

1) Appear in a well motivated and consistent physical model;

Kerr: General Relativity

2) Have a dynamical formation mechanism;

Kerr: gravitational collapse

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Kerr: mode stability established (B. F. Whiting, J. Math. Phys. 30 (1989) 1301)

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Crucially, moreover, it must give the right phenomenology:

1) all electromagnetic observables  
(X-ray spectrum, shadows, QPOs, star orbits,...);

2) correct Gravitational wave templates

*No clear  
tension between  
observations and  
the Kerr model*

# A key feature to assess the strong field phenomenology: Fundamental Photon orbits (define the black hole shadow)

First “image” of the black hole shadow may be around the corner:



**ALL OVER THE MAP** Capturing a black hole takes a planet-sized telescope — or a planet covered in telescopes working together. Shown are the various international sites participating, or expected to participate, in Event Horizon Telescope observations.

- Planned
- Already used

Falcke, Melia, Agol, *Astrophys. J.* 528, L13 (2000);  
A. E. Broderick and A. Loeb, *MNRAS* 367, 905 (2006);  
S. Doeleman et al., 0906.3899

The edge of the shadow is determined by the

## Fundamental Photon Orbits

Cunha, C.H., Radu, PRD 96 (2017) 024039

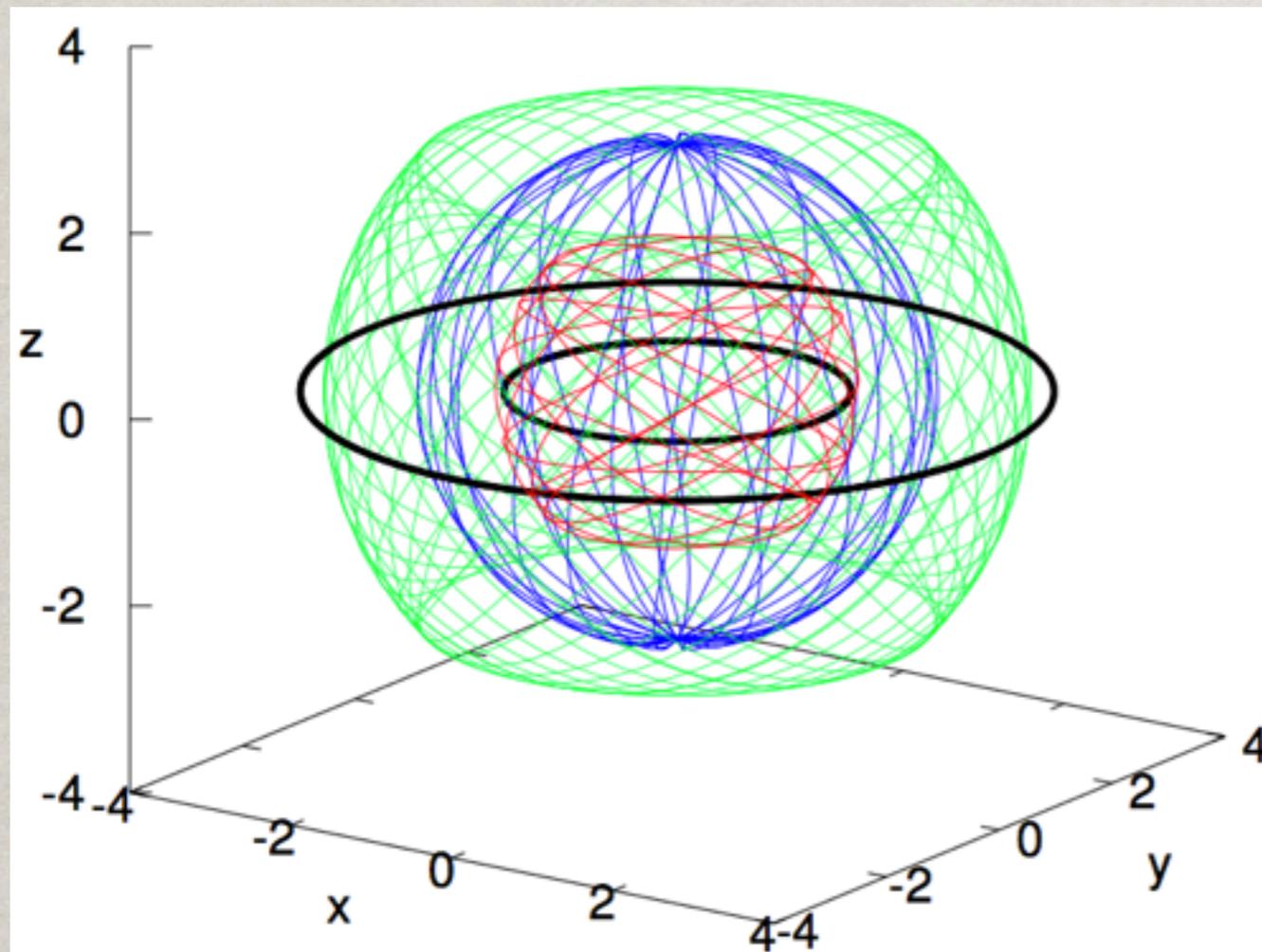
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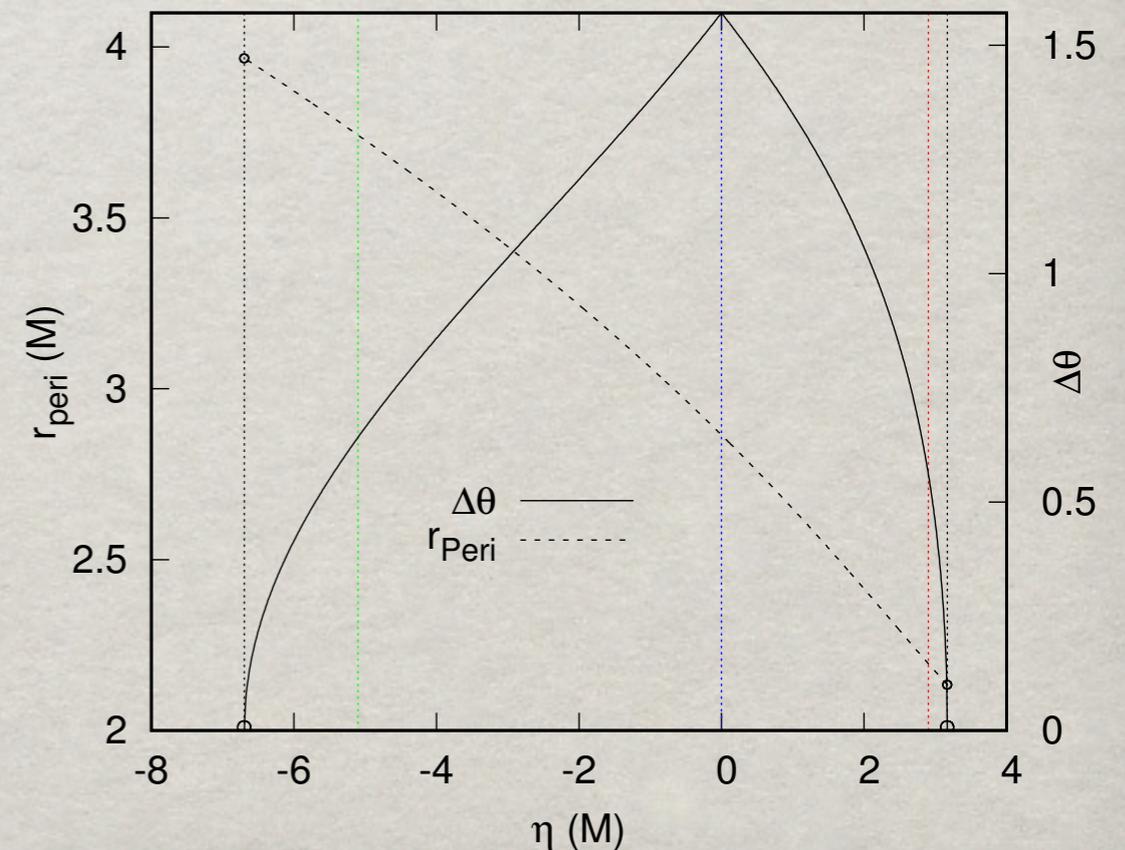
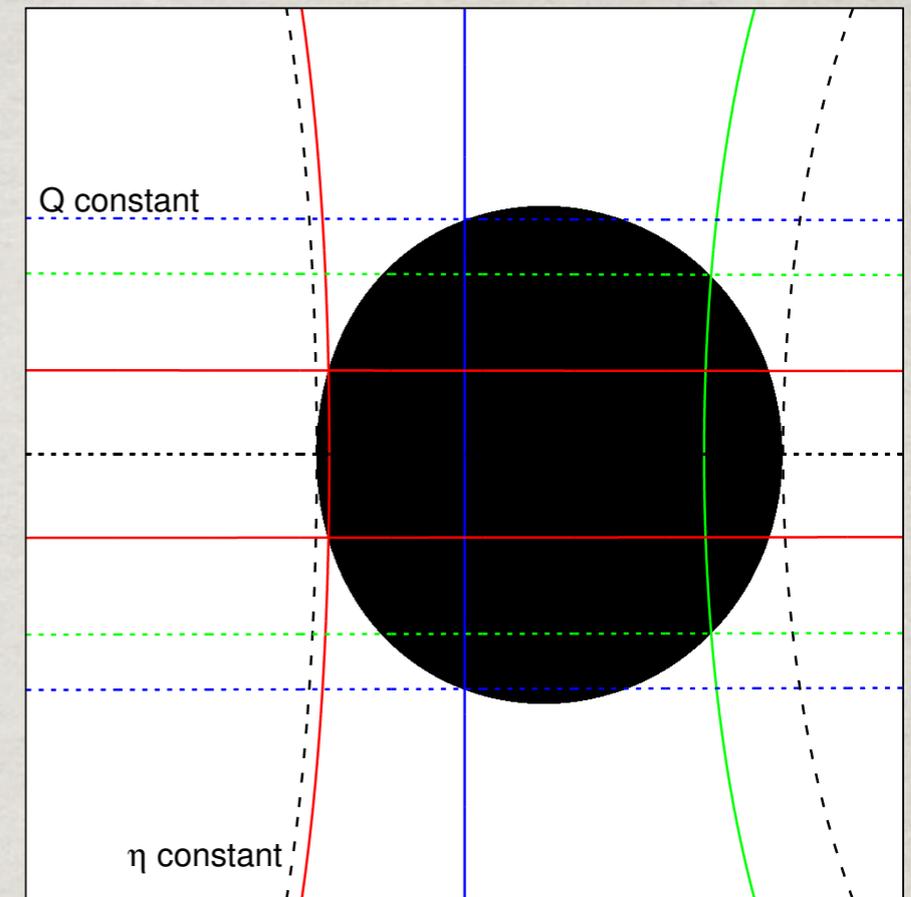
Relate to quasi-normal ringing

Goebel, Astrophys. J. 172 (1972) L95

Cardoso, Franzin and Pani, PRL 116 (2016) 171101



$j \sim 0.82$



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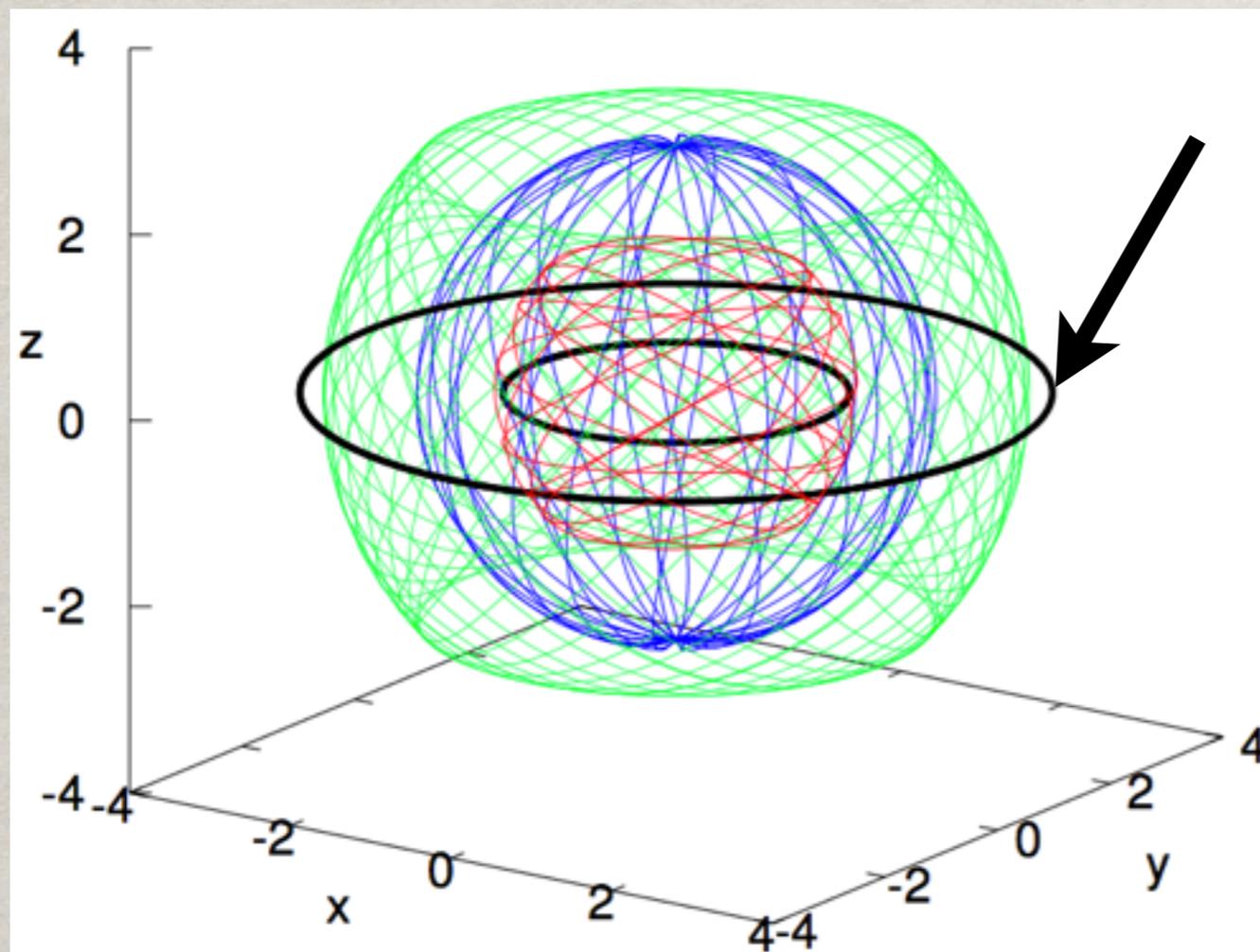
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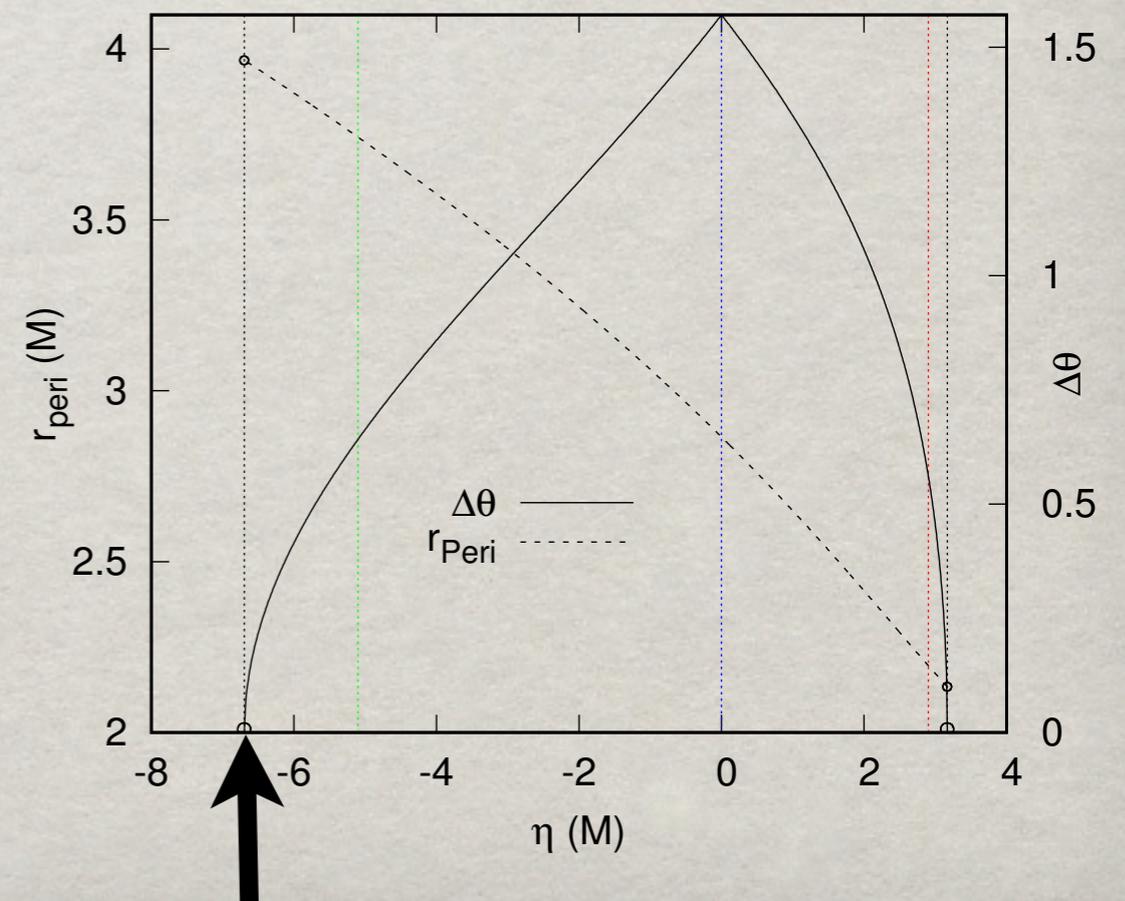
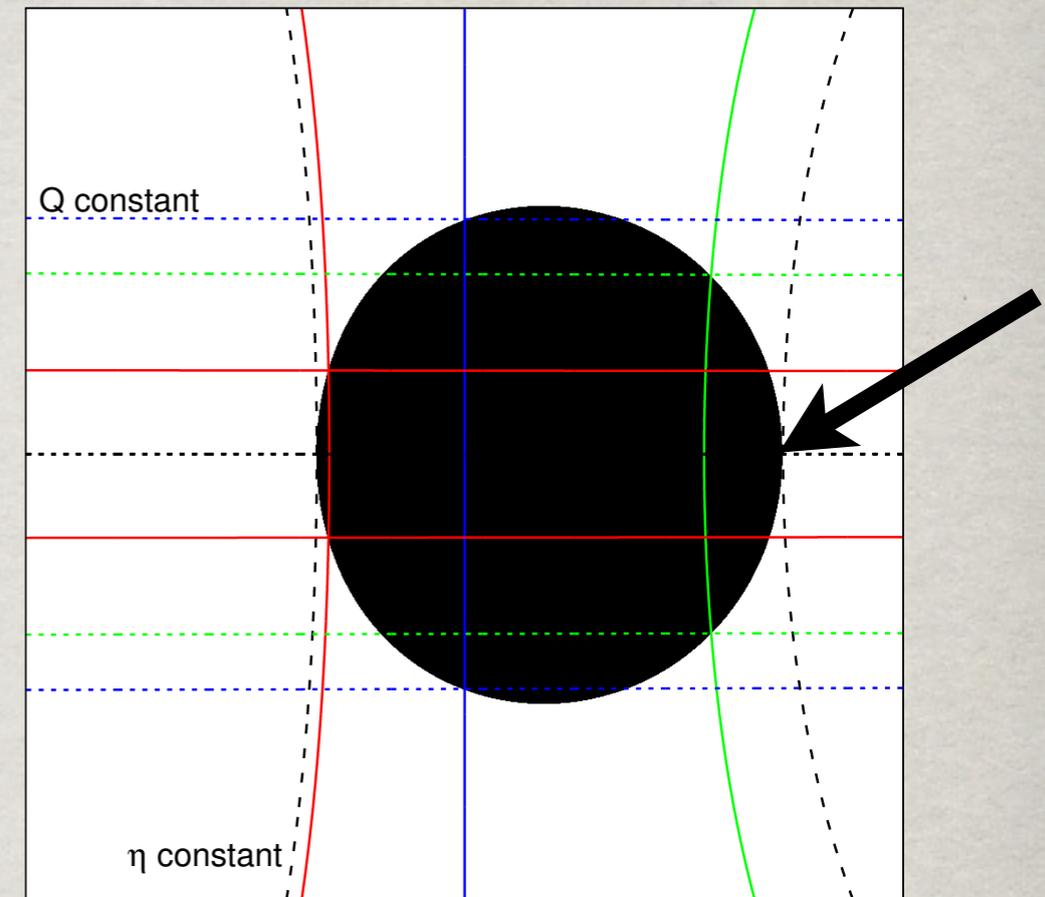
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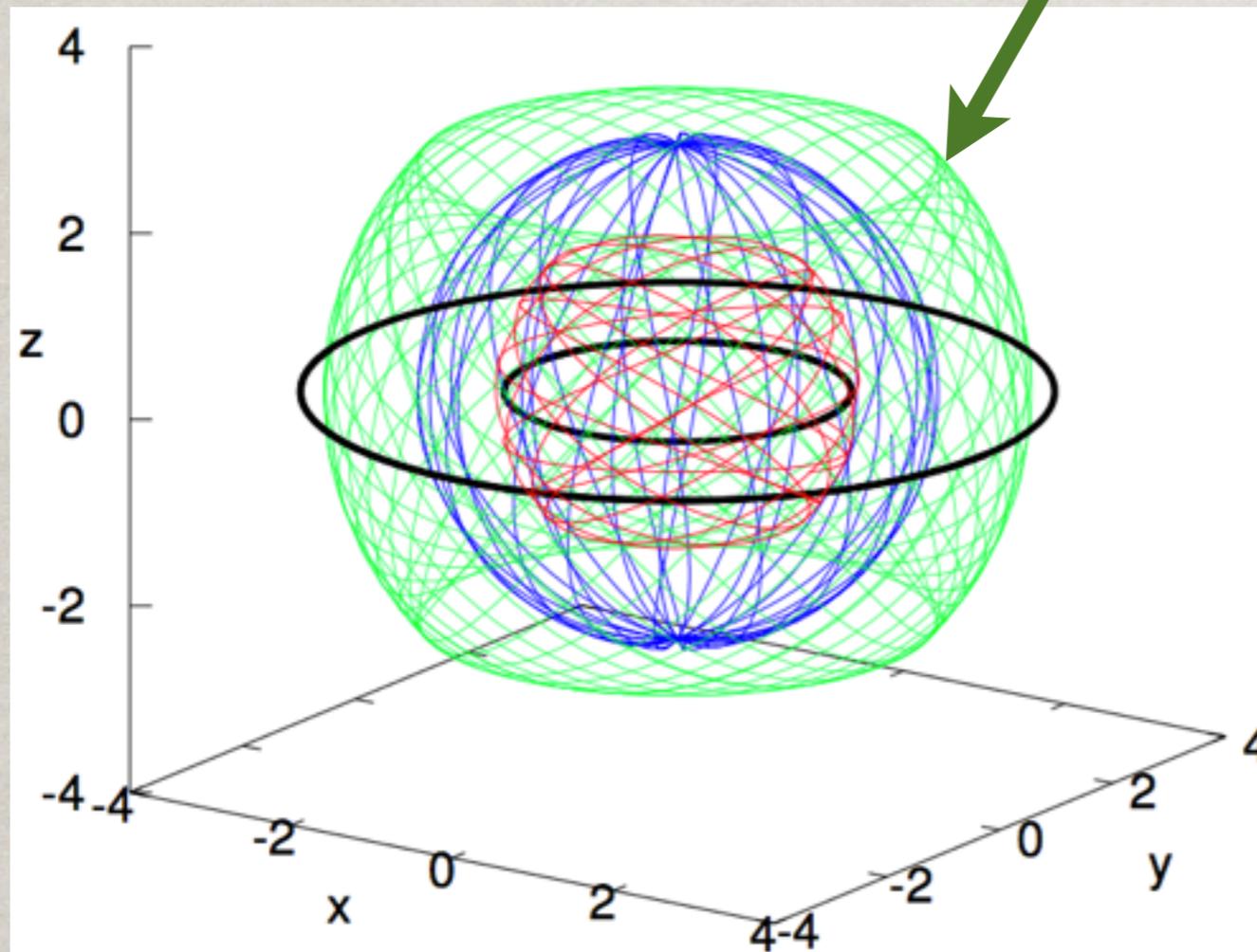
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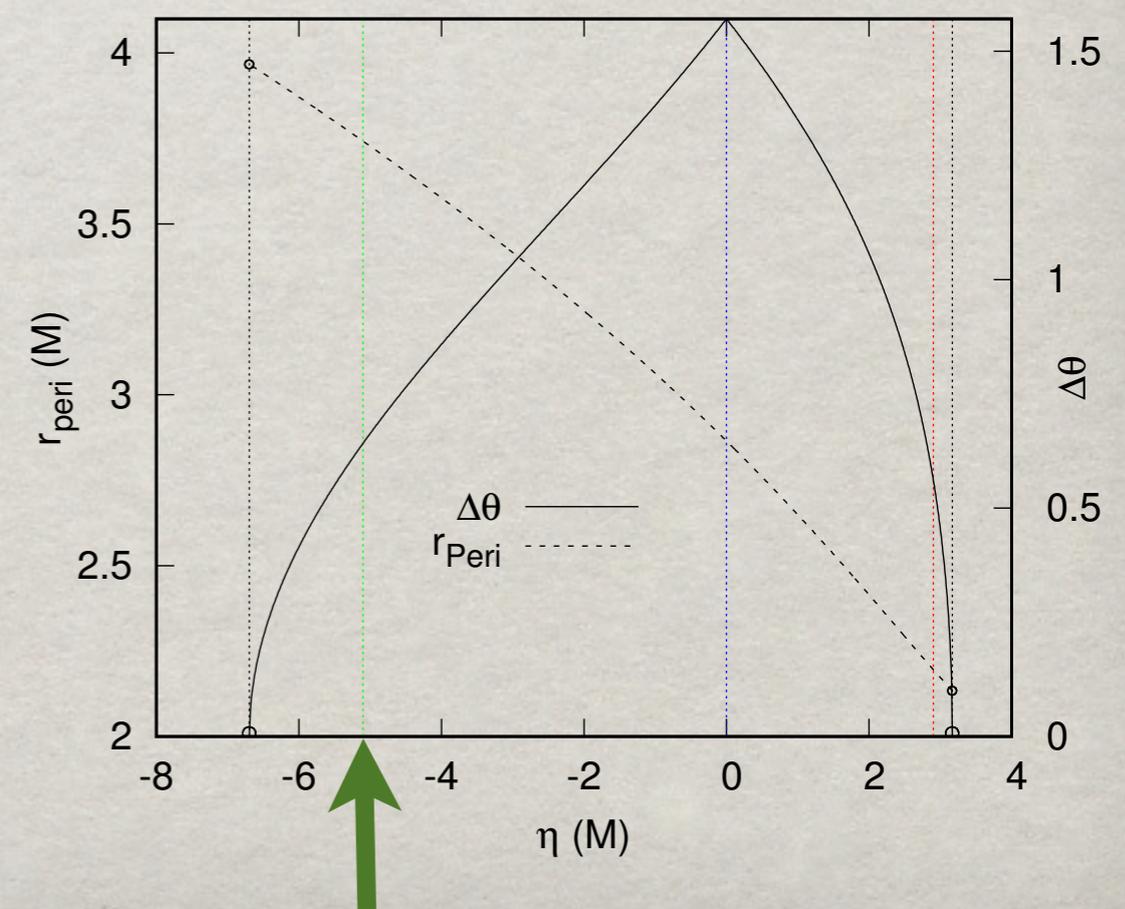
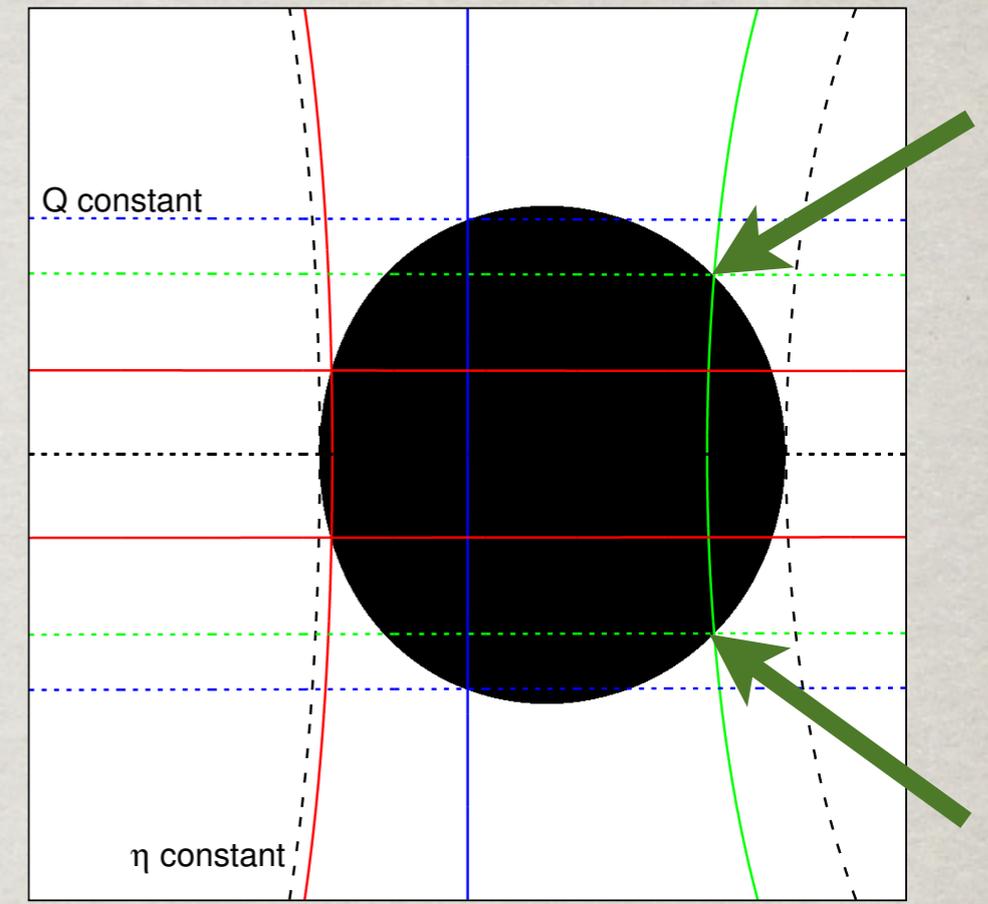
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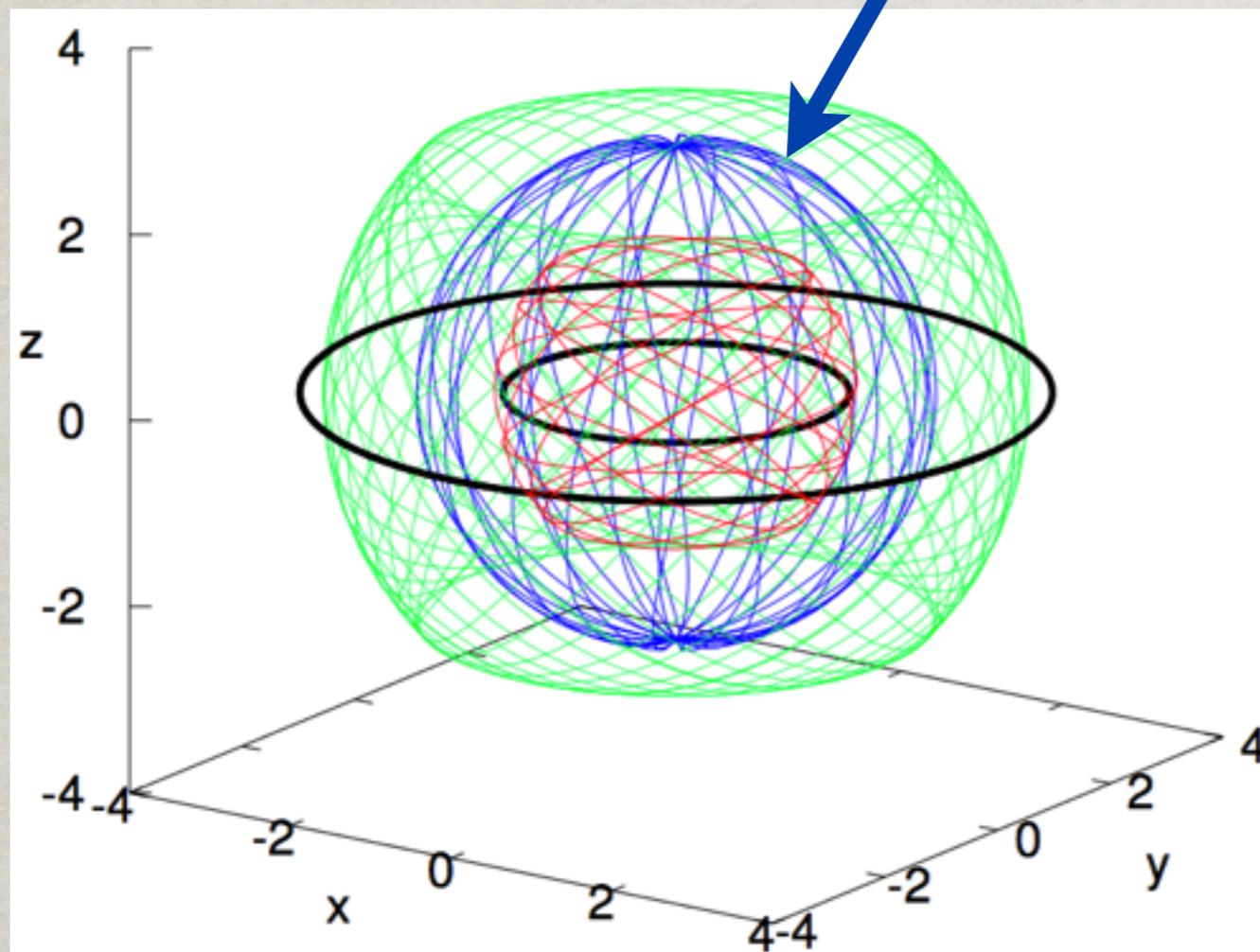
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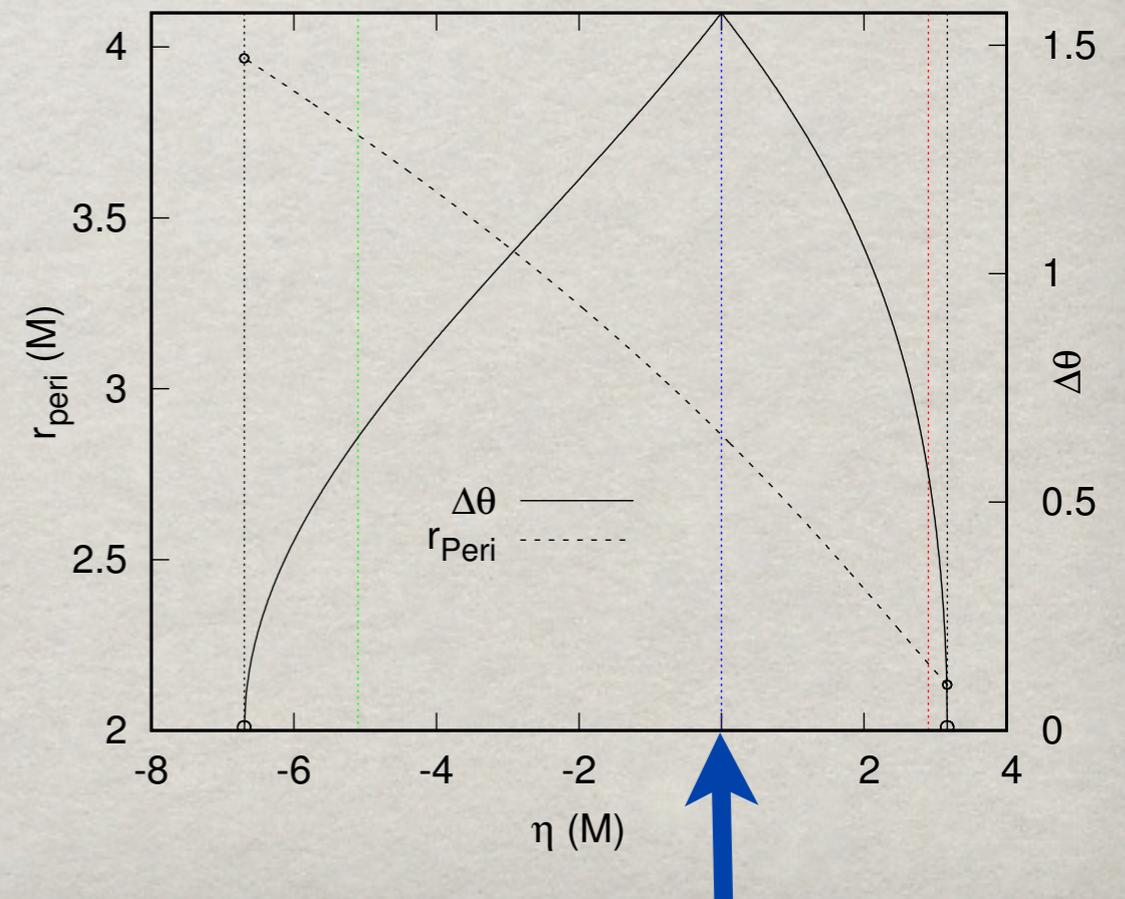
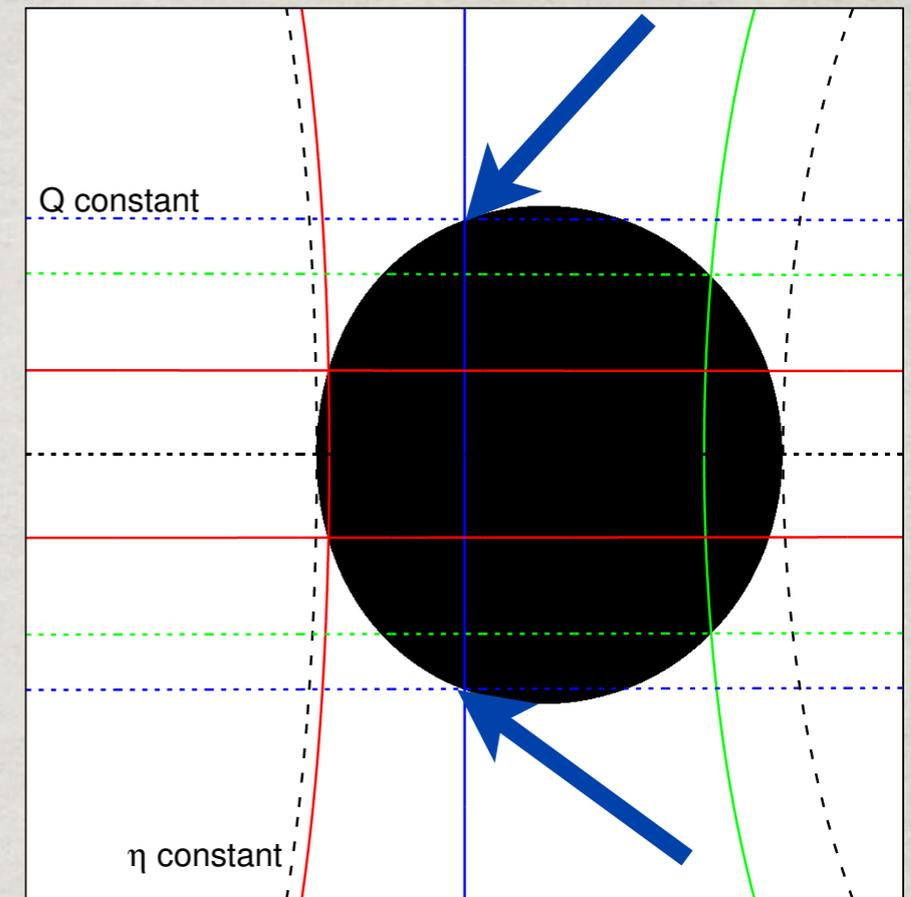
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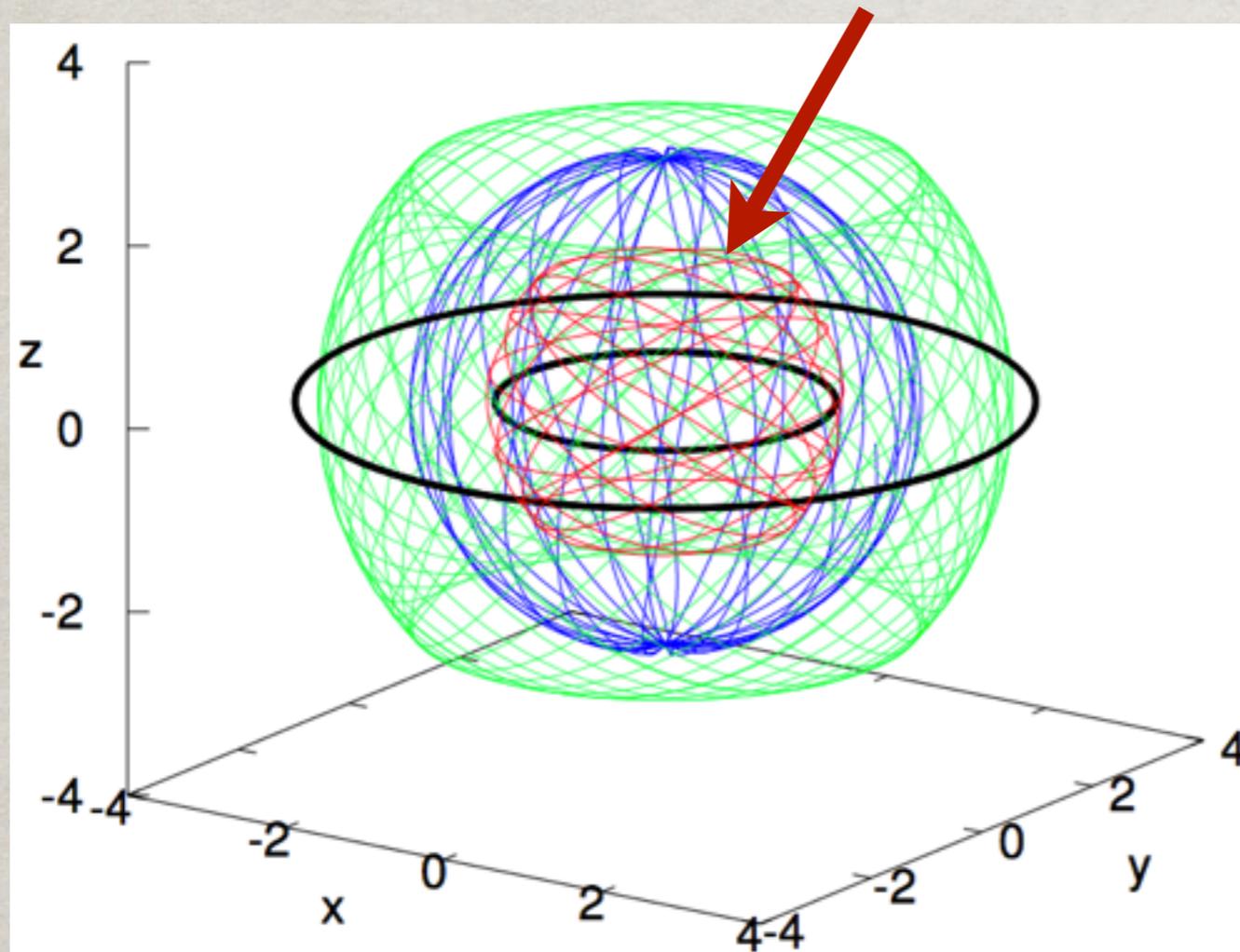
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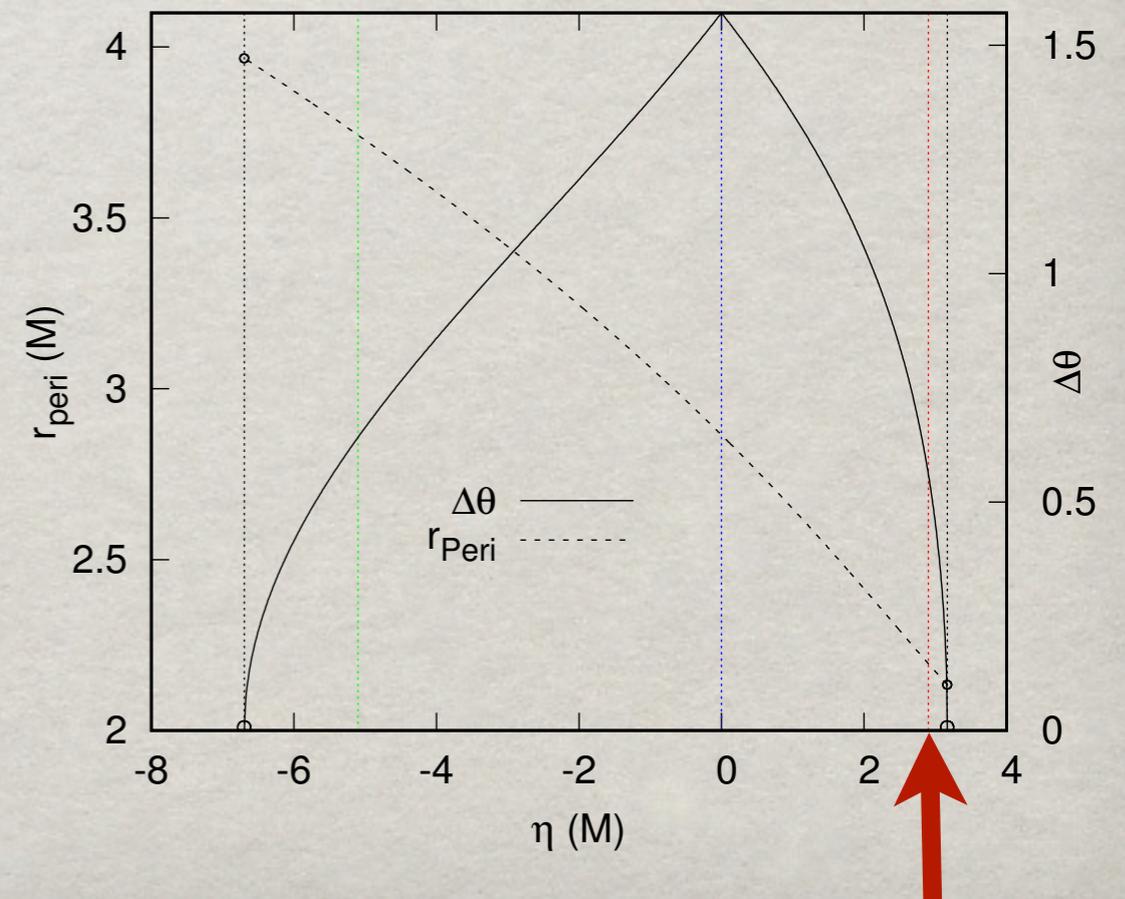
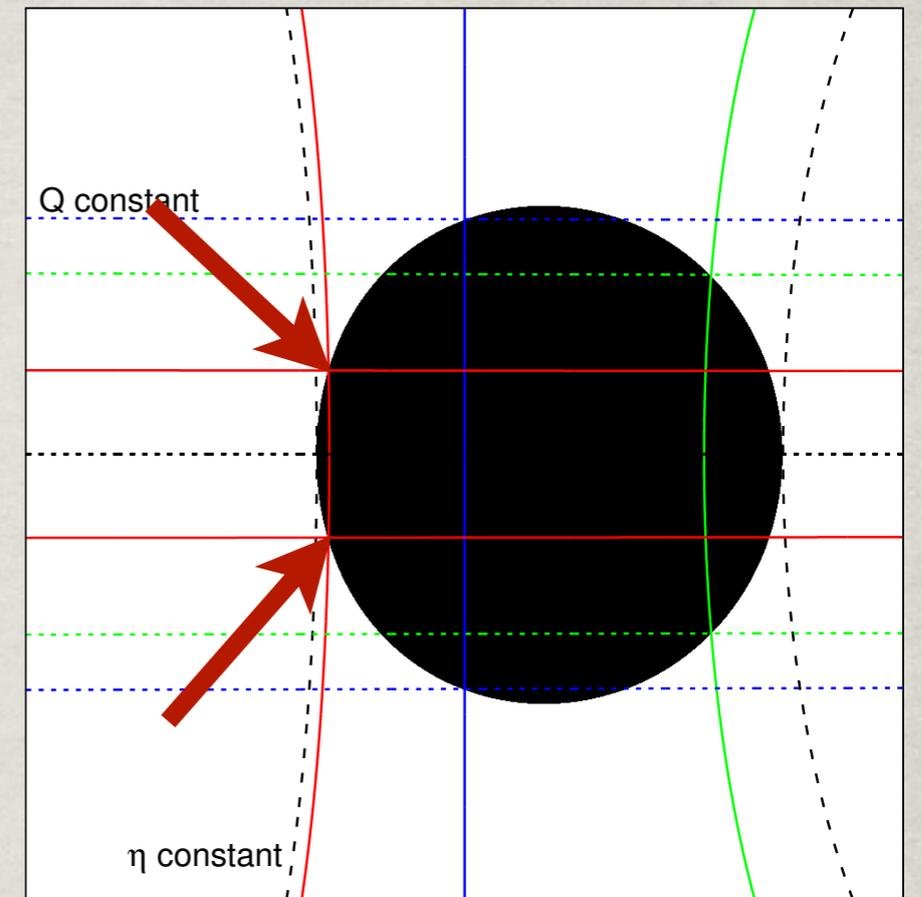
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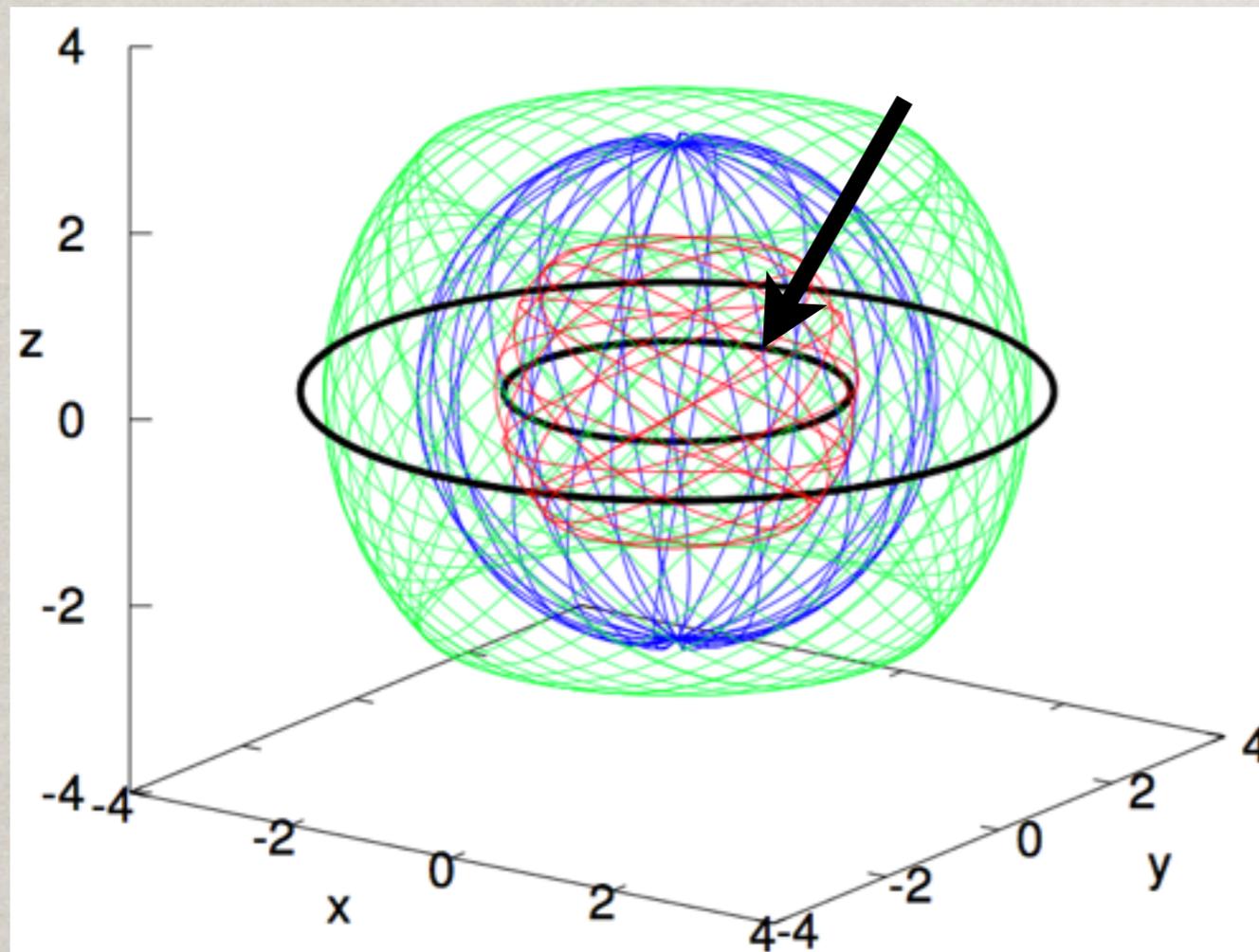
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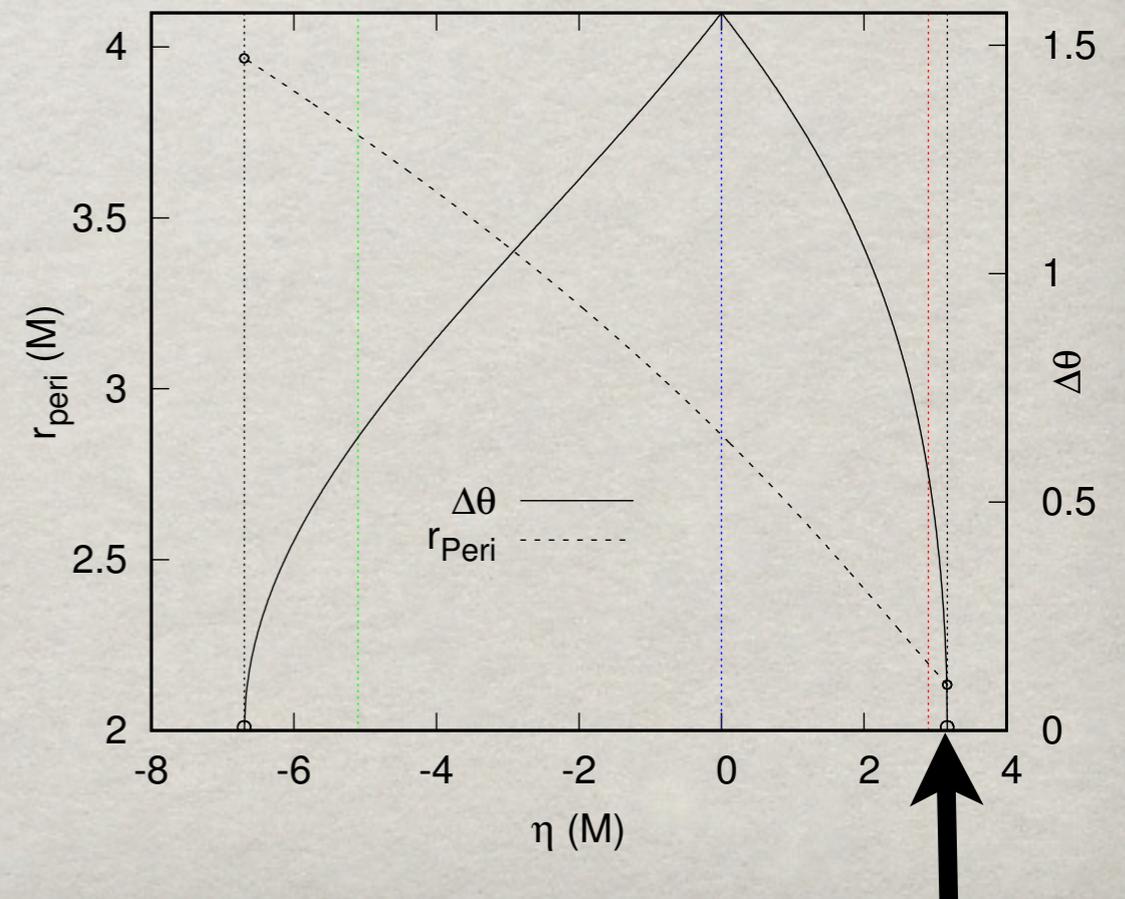
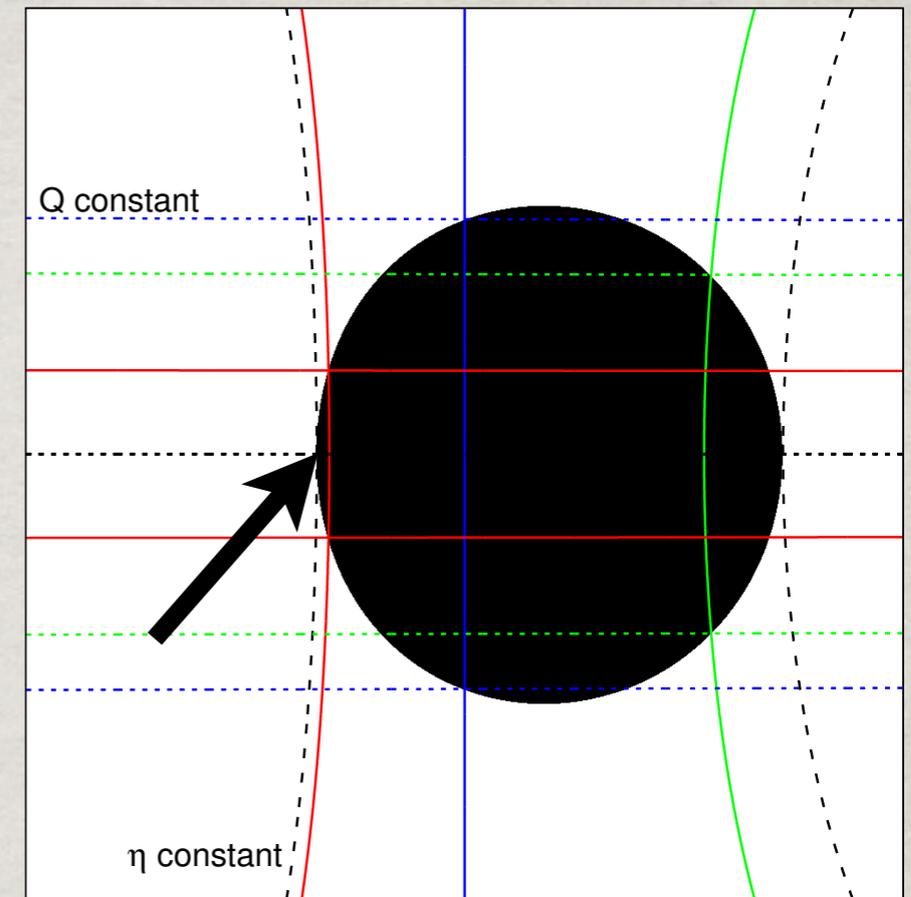
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Are there other theoretically sound models  
that have different black holes ?  
How different from Kerr is the phenomenology?

# Many no-scalar-hair theorems:

(only scalars, D=4, asymptotically flat)

Theory Lagrangian density $\mathcal{L}$	No-hair theorem	Known scalar hairy BHs with regular geometry on and outside $\mathcal{H}$ (primary or secondary hair; regularity)
Scalar-vacuum $\frac{1}{4}R - \frac{1}{2}\nabla_{\mu}\Phi\nabla^{\mu}\Phi$	Chase <sup>22</sup>	
Massive-scalar-vacuum $\frac{1}{4}R - \frac{1}{2}\nabla_{\mu}\Phi\nabla^{\mu}\Phi - \frac{1}{2}\mu^2\Phi^2$	Bekenstein <sup>11</sup>	
Massive-complex-scalar-vacuum $\frac{1}{4}R - \nabla_{\mu}\Phi^*\nabla^{\mu}\Phi - \mu^2\Phi^*\Phi$	Pena– Sudarsky <sup>61</sup>	Herdeiro–Radu <sup>136, 137</sup> (primary, regular); generalizations: <sup>159</sup>
Conformal-scalar-vacuum $\frac{1}{4}R - \frac{1}{2}\nabla_{\mu}\Phi\nabla^{\mu}\Phi - \frac{1}{12}R\Phi^2$	Xanthopoulos– Zannias <sup>32</sup> Zannias <sup>33</sup>	Bocharova–Bronnikov–Melnikov– Bekenstein (BBMB) <sup>16–18</sup> (secondary, diverges at $\mathcal{H}$ ); generalizations: <sup>87</sup>
V-scalar-vacuum $\frac{1}{4}R - \frac{1}{2}\nabla_{\mu}\Phi\nabla^{\mu}\Phi - V(\Phi)$	Heusler <sup>46, 47, 50</sup> Bekenstein <sup>26</sup> Sudarsky <sup>51</sup>	Many, with non-positive definite potentials: <sup>71–75, 78–80</sup> (typically secondary, regular)
P-scalar-vacuum $\frac{1}{4}R + P(\Phi, X)$	Graham– Jha <sup>62</sup>	
Einstein-Skyrme $\frac{1}{4}R - \frac{1}{2}\nabla_{\mu}\Phi^a\nabla^{\mu}\Phi^a$ $-\kappa \nabla_{[\mu}\Phi^a\nabla_{\nu]}\Phi^b ^2$		Droz–Heusler–Straumann <sup>126</sup> (primary but topological; regular); generalizations: <sup>129, 131</sup>
Scalar-tensor theories $\varphi\hat{R} - \frac{\omega(\varphi)}{\varphi}\hat{\nabla}_{\mu}\varphi\hat{\nabla}^{\mu}\varphi - U(\varphi)$	Hawking <sup>27</sup> Saa <sup>34, 35</sup> Sotiriou– Faraoni <sup>31</sup>	
Horndeski/Galileon theories Full $\mathcal{L}$ in eq. (41)	Hui– Nicolis <sup>45</sup>	Sotiriou-Zhou <sup>43</sup> (secondary; regular) Babichev–Charmousis <sup>88, 90</sup> (secondary <sup>88</sup> or primary, <sup>90</sup> diverges at $\mathcal{H}^+$ or $\mathcal{H}^-$ ); generalizations: <sup>91–93</sup>

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GR  
example



beyond GR  
example



## **2) Black Holes beyond Kerr**

## a) In General Relativity

Massive-complex-scalar-vacuum:

$$\mathcal{S} = \frac{1}{4\pi} \int d^4x \sqrt{-g} \left( \frac{R}{4} - \nabla_\alpha \Phi^* \nabla^\alpha \Phi - \mu^2 |\Phi|^2 \right)$$

There are BH solutions:

- **within GR** (not alternative theories of gravity);
- with matter **obeying all energy conditions**;
- which can yield **distinct phenomenology**;

which are:

- asymptotically flat
- regular on and outside the horizon
- continuously connecting to the Kerr solution
- continuously connected to relativistic Bose-Einstein condensates (boson stars)
  - with an independent scalar charge (primary hair)
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**Black Holes with synchronised hair**

CH and Radu, PRL112(2014)221101

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$-V(|\Phi|)$

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$$\mathcal{S} = \frac{1}{4\pi} \int d^4x \sqrt{-g} \left( \frac{R}{4} - \nabla_\alpha \Phi^* \nabla^\alpha \Phi - \mu^2 |\Phi|^2 \right)$$

$$-V(|\Phi|) = -\lambda \Phi^4$$

New scale  
could single out  
BHs of a certain size  
to become "hairy"

CH, Radu, Rúnarsson, PRD92(2015)084059

There are BH solutions:

- **within GR** (not alternative theories of gravity);
- with matter **obeying all energy conditions**;
- which can yield **distinct phenomenology**;

also  
Kleihaus, Kunz and Yazadjiev  
PLB744(2015)406

which are:

- asymptotically flat
- regular on and outside the horizon
- continuously connecting to the Kerr solution
- continuously connected to relativistic Bose-Einstein condensates (boson stars)
  - with an independent scalar charge (primary hair)
- Can form dynamically and be sufficiently long lived

**Black Holes with synchronised hair**

CH and Radu, PRL112(2014)221101

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CH and Radu, PRL112(2014)221101

**Existence proof**

Chodosh and Shlapentokh-Rothman,  
CMP356(2017)1155

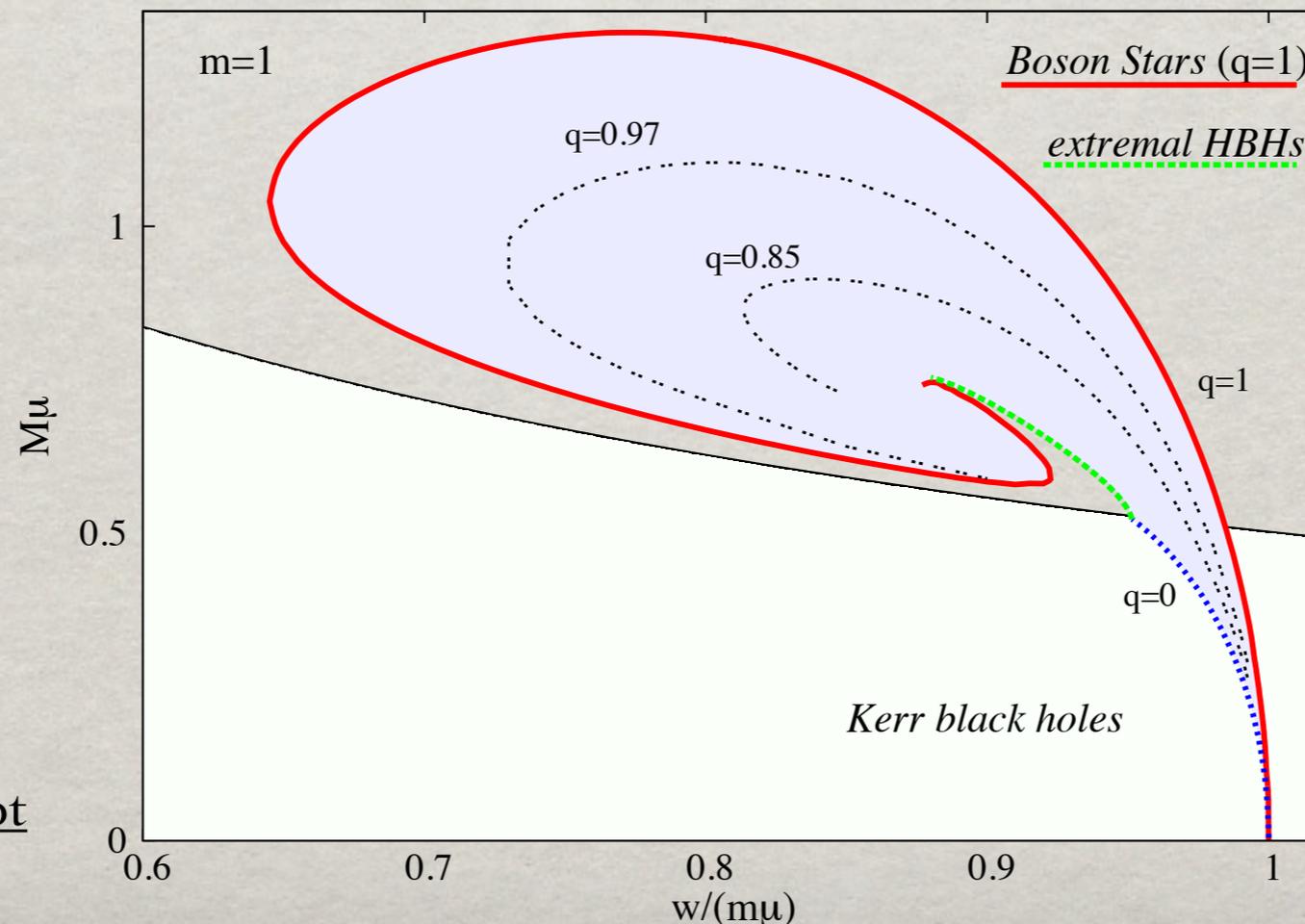
# Black holes with synchronised scalar hair

$$\mathcal{S} = \frac{1}{4\pi} \int d^4x \sqrt{-g} \left( \frac{R}{4} - \nabla_\alpha \Phi^* \nabla^\alpha \Phi - \mu^2 |\Phi|^2 \right)$$

Ansatz:

$$ds^2 = -e^{2F_0(r,\theta)} N dt^2 + e^{2F_1(r,\theta)} \left( \frac{dr^2}{N} + r^2 d\theta^2 \right) + e^{2F_2(r,\theta)} r^2 \sin^2 \theta (d\varphi - W(r,\theta) dt)^2 \quad N = 1 - \frac{r_H}{r}$$

$$\Phi = \phi(r, \theta) e^{i(m\varphi - \omega t)}$$



$$\Omega_H = \frac{\omega}{m}$$

“synchronisation”  
condition

Data available online at:  
<http://gravitation.web.ua.pt>

Can they form dynamically ?

Formation from Kerr

In the presence of these ultra-light fields,  
vacuum Kerr black holes are **unstable**  
(against superradiance).

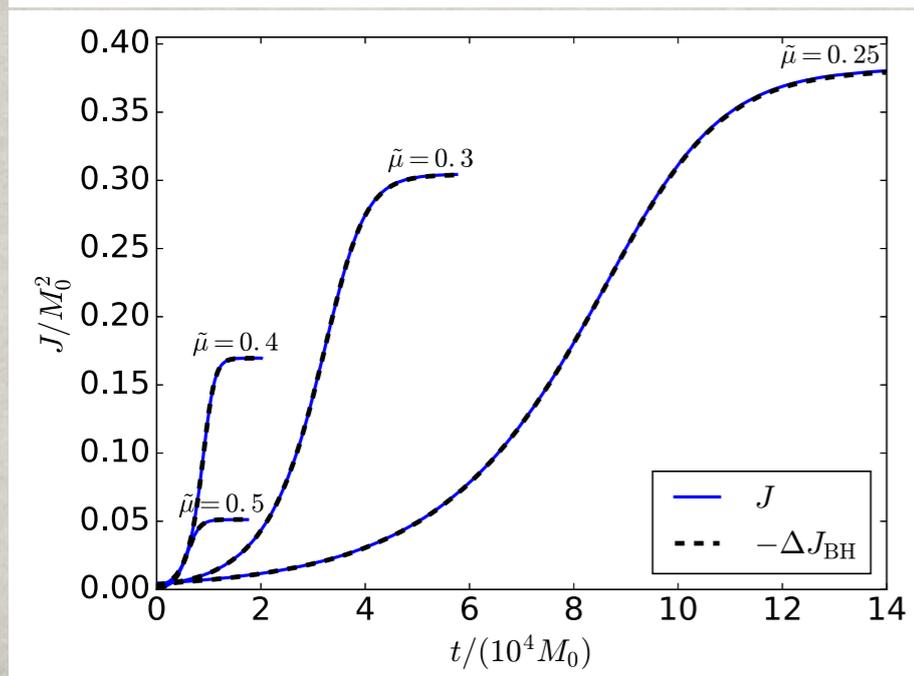
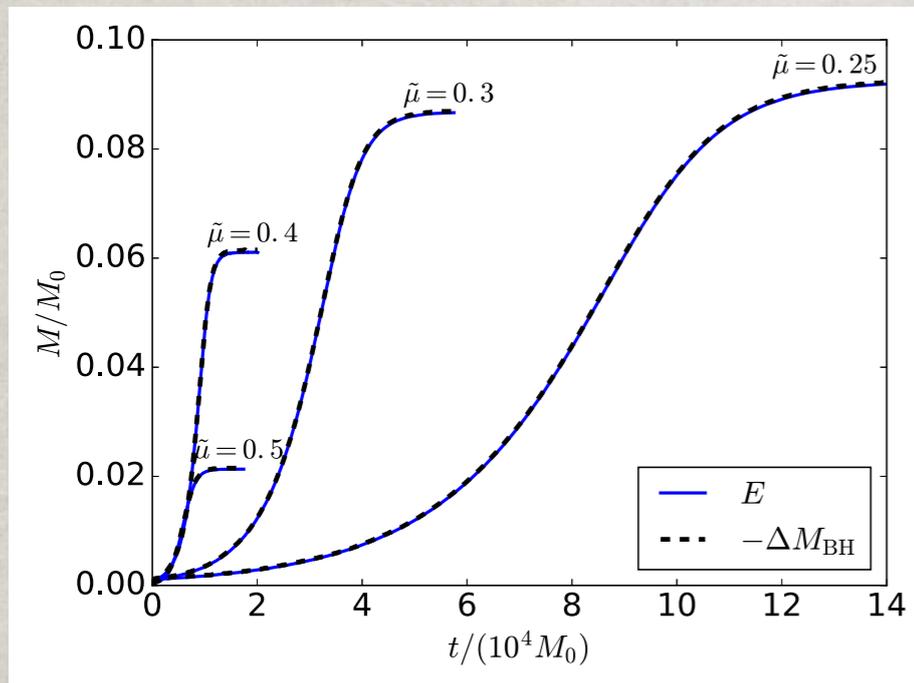
The instability is most efficient when the  
Compton wavelength  $\sim$  Schwarzschild radius.

What is the endpoint of this instability?

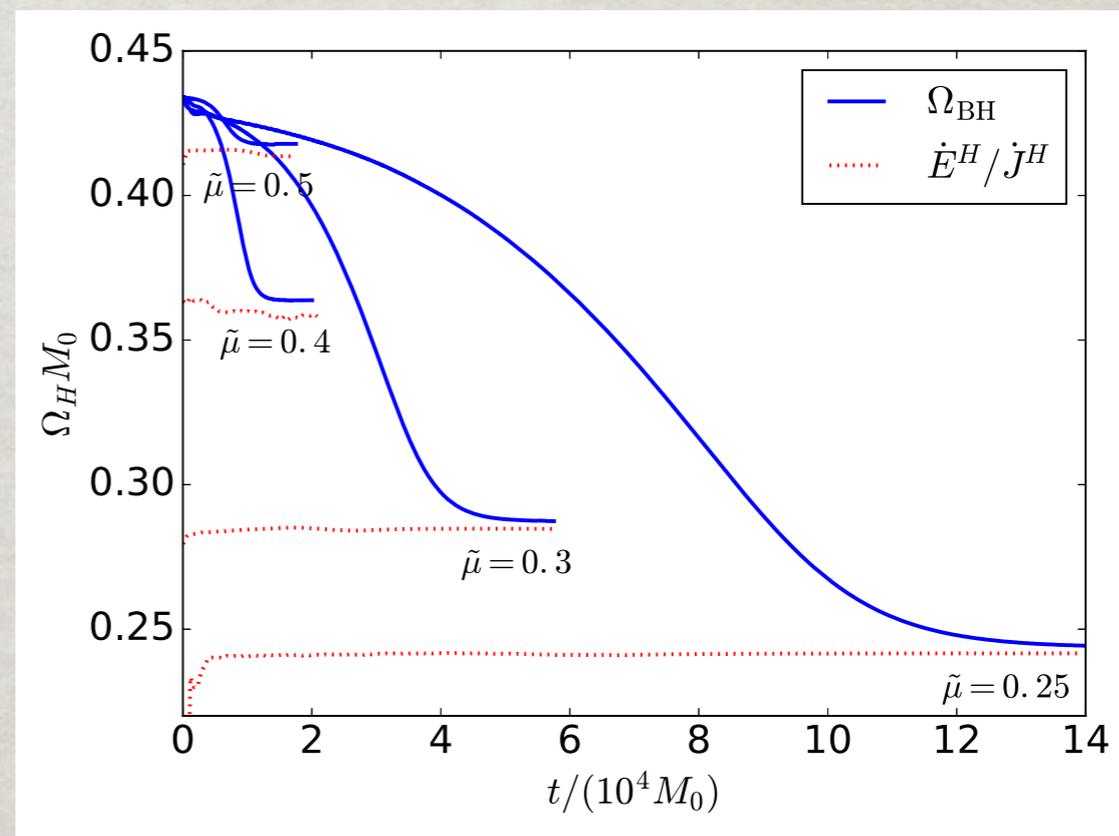
# Recent dynamical evidence (for the cousin Proca model) shows the process reaches an equilibrium state...

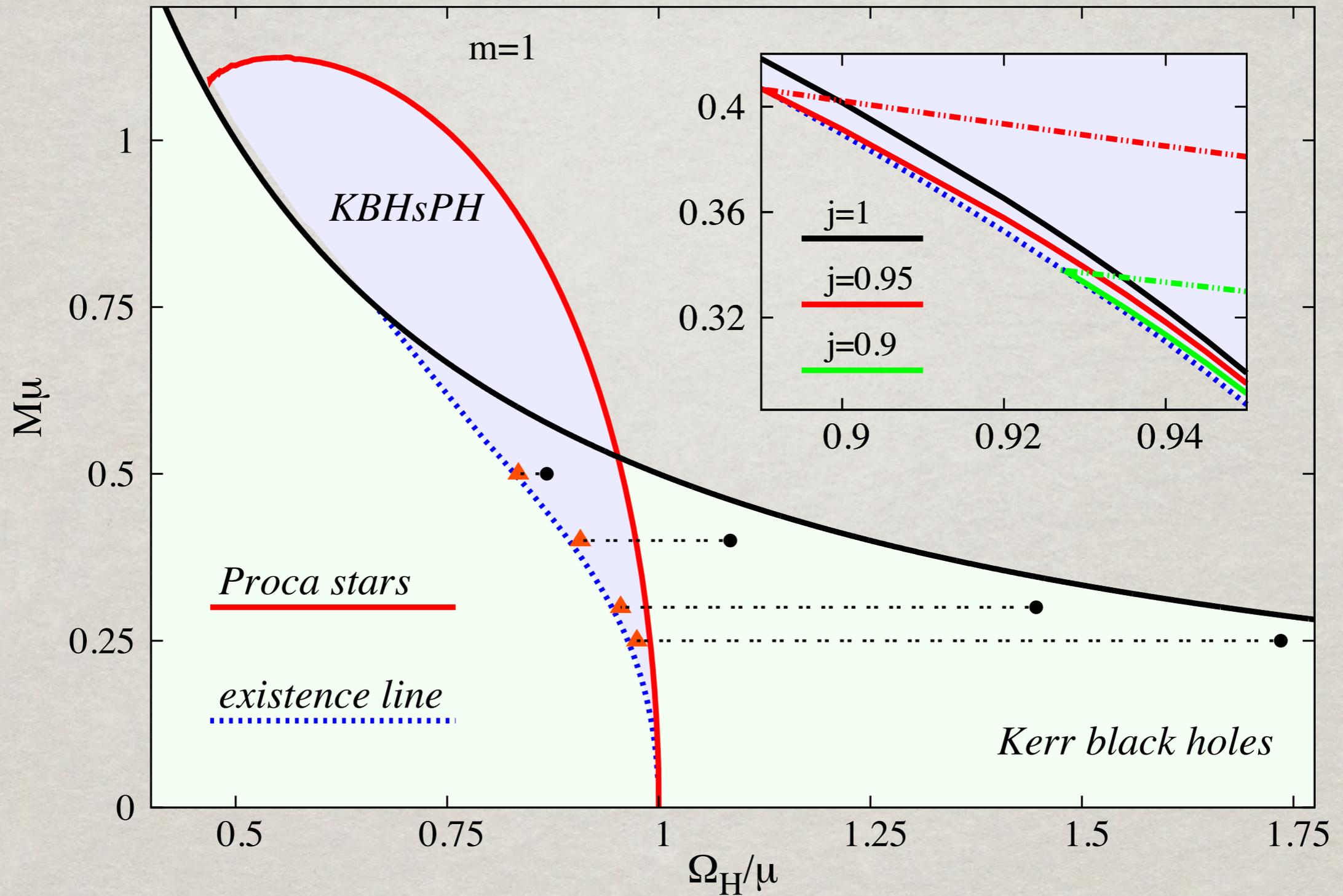
East and Pretorius, PRL119(2017)041101

## Mass and angular momentum in “hair”



## Black hole spin down and “synchronisation”

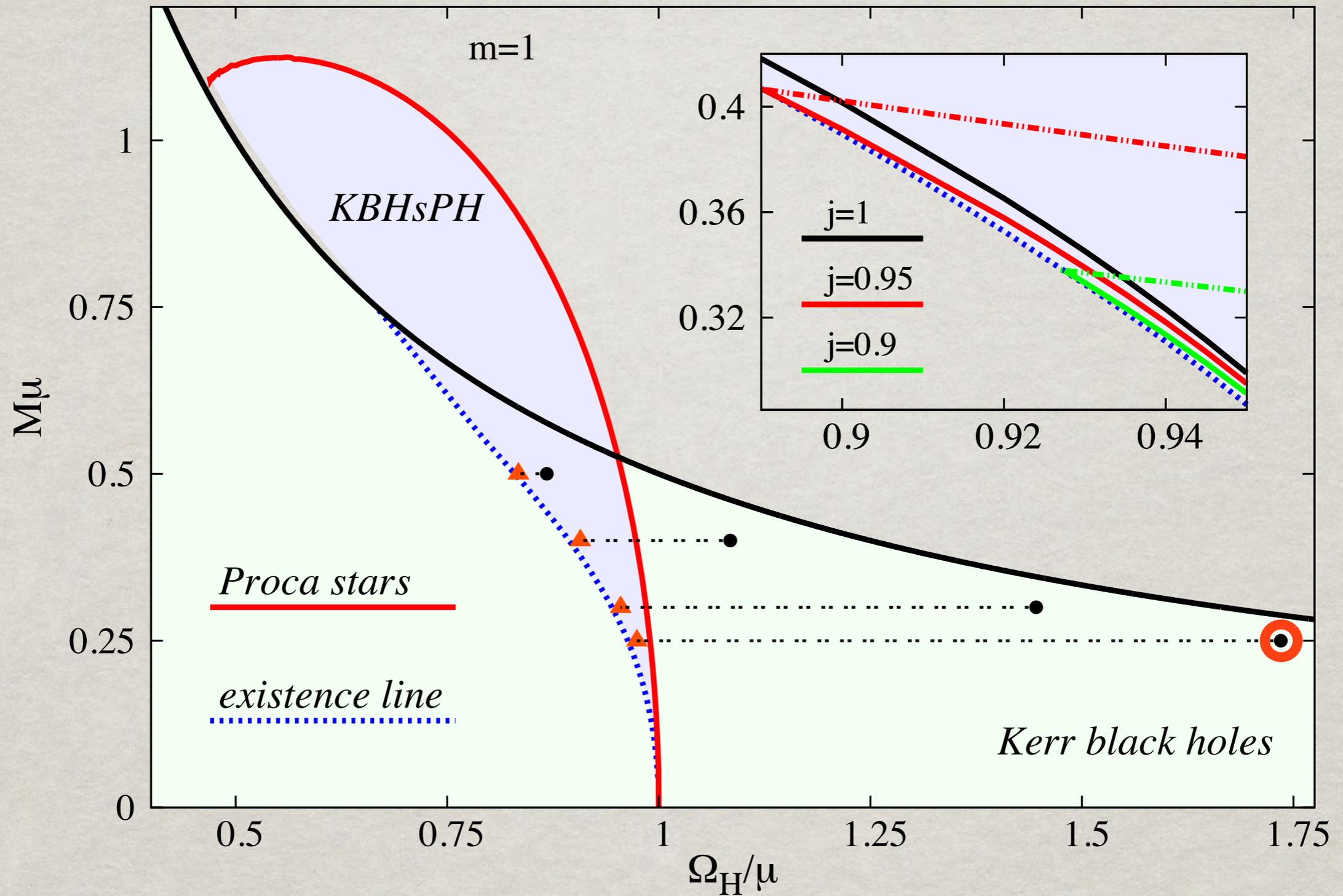




... which is a hairy black hole

CH, Radu, PRL 119 (2017) 261101

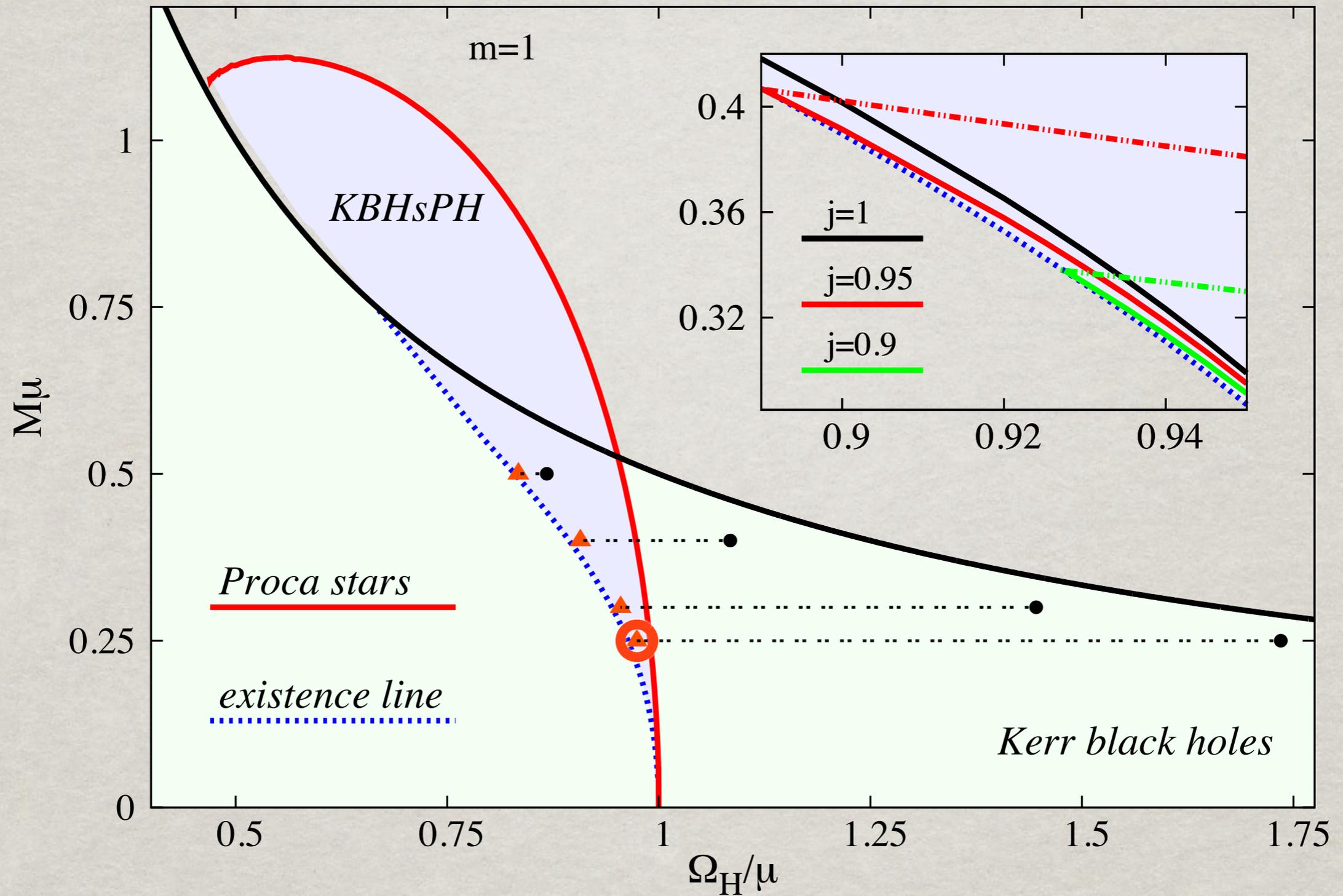
Dolan, Physics10(2017)83



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CH, Radu, PRL 119 (2017) 261101

Dolan, Physics10(2017)83



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CH, Radu, PRL 119 (2017) 261101

Dolan, Physics10(2017)83

Kerr  $\xrightarrow{\Delta t}$  Hairy black hole

But is this the  
end of the process?

Kerr  $\xrightarrow{\Delta t}$  Hairy black hole

But is this the  
end of the process?

- These hairy black holes have an ergoregion themselves [CH, Radu, PRD 89 \(2014\) 124018](#);
- Suggests they are also afflicted by superradiant instabilities of higher “m” modes (when in the superradiant range);

Kerr  $\xrightarrow{\Delta t}$  Hairy black hole

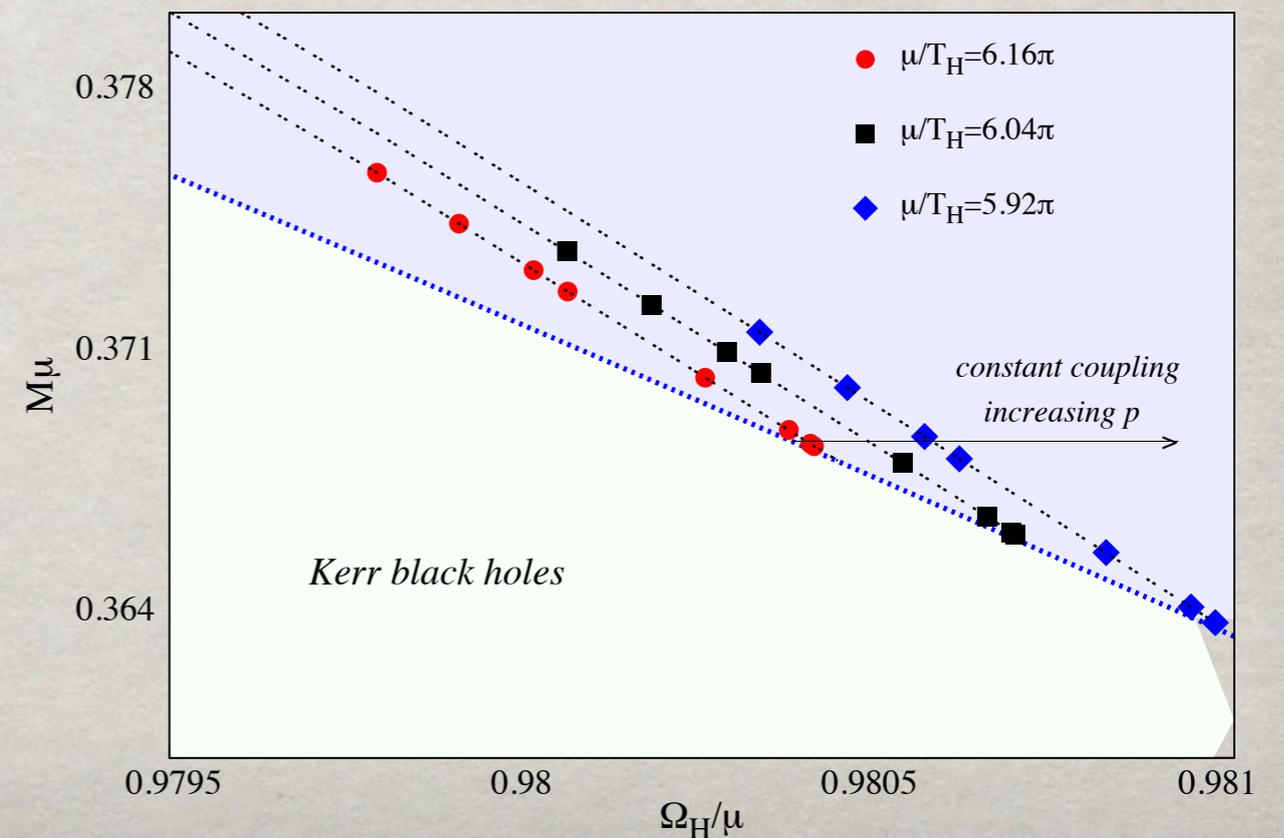
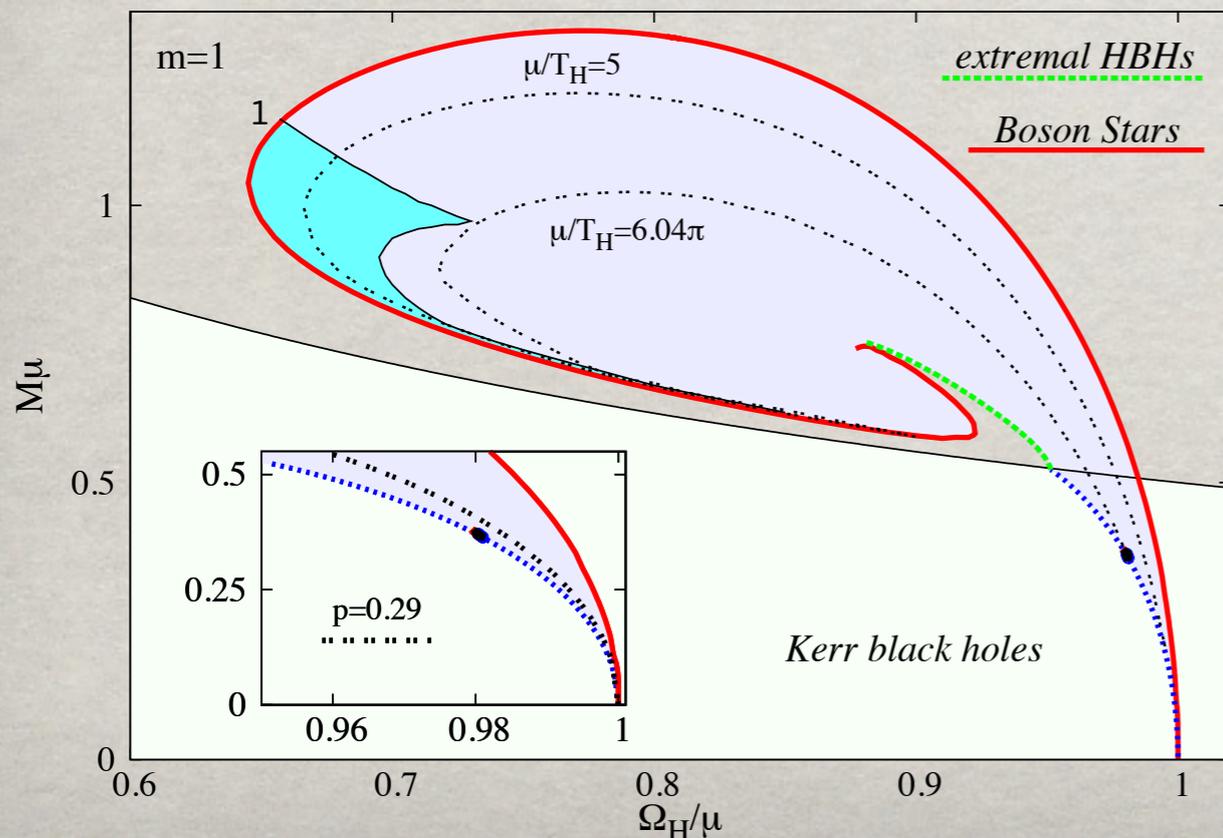
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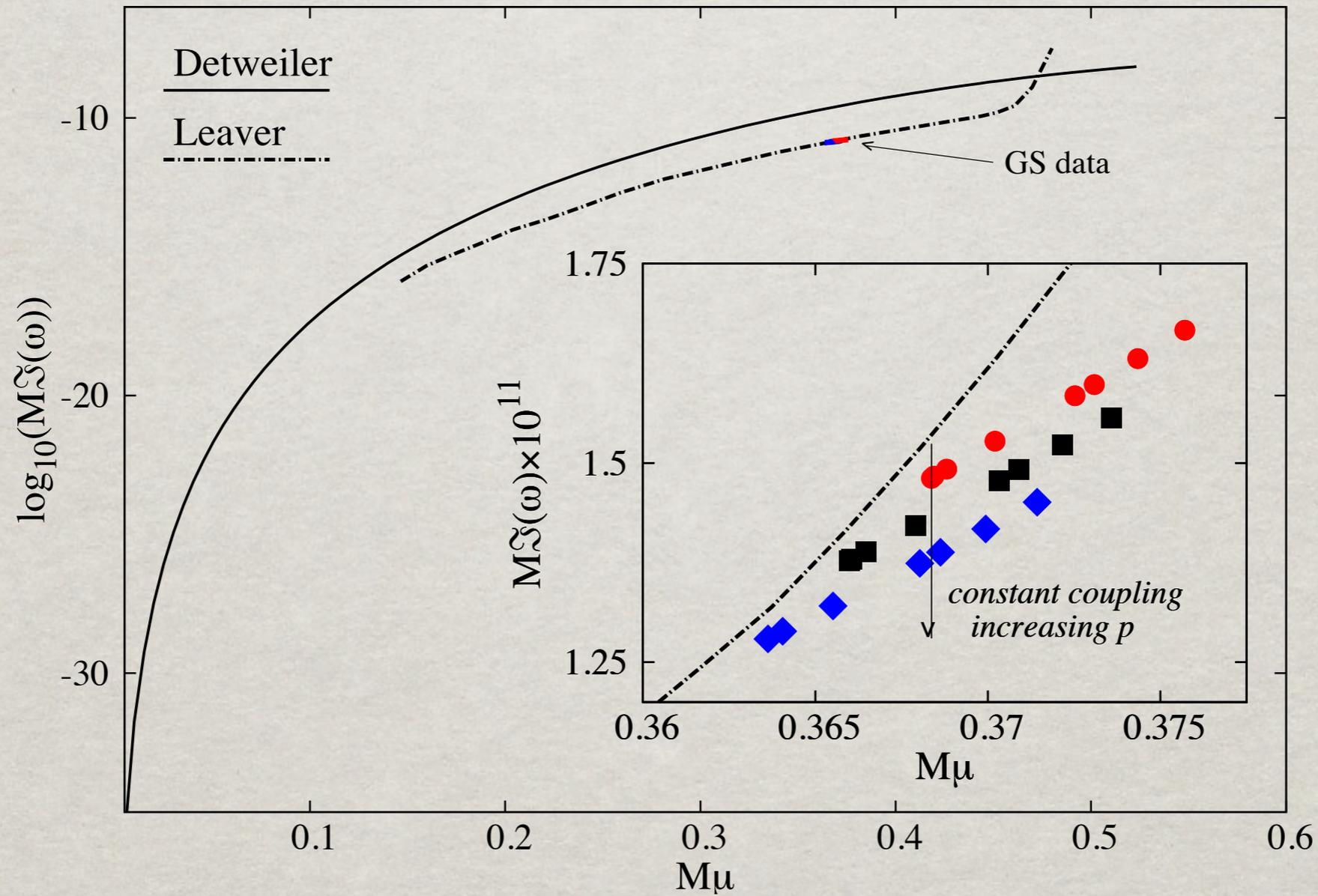
This was confirmed by [Ganchev and Santos 1711:08464](#)

- 1) the instability found is the anticipated superradiant instabilities
- 2) the claims therein concerning timescales are non-generic [Degollado, CH, Radu, 1802.07266](#)

All have less than 2% of energy in “hair”

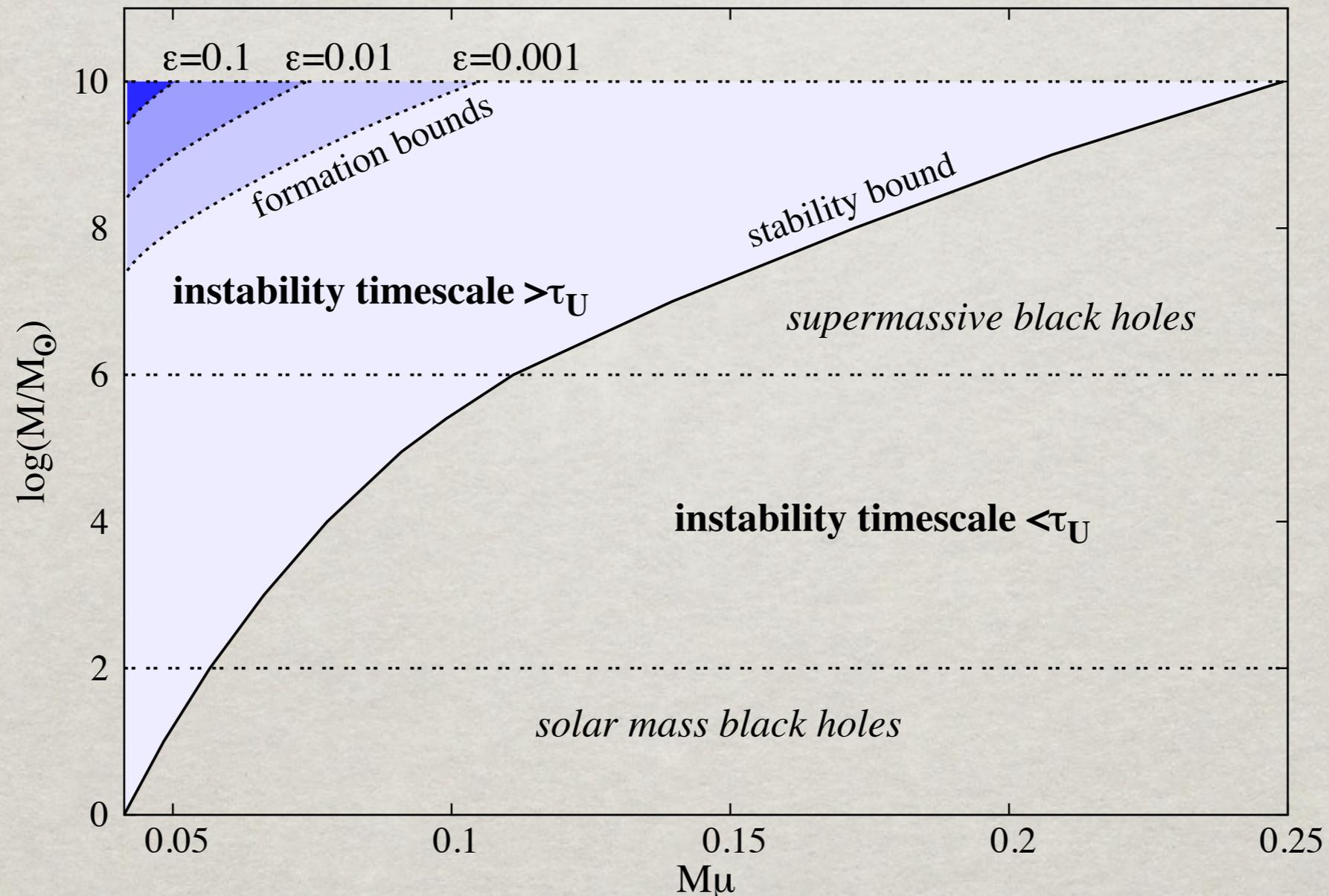


Observation 1 about timescales [Degollado, CH, Radu, 1802.07266](#):  
For fixed coupling, increasing “hairiness” decreases strength of instability.



## Observation 2 about timescales [Degollado, CH, Radu, 1802.07266](#):

There are hairy BHs for which the instability timescale is larger than the age of the Universe.



A conservative estimate of the Astrophysically viable region

Kerr  $\xrightarrow[\text{(astrophysical time scale)}]{\Delta t}$  Hairy black hole

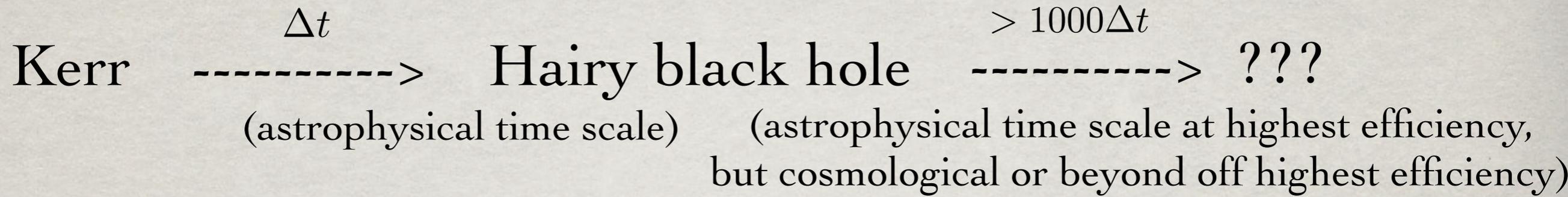
2) Is this the end of the process?

Kerr  $\xrightarrow[\text{(astrophysical time scale)}]{\Delta t}$  Hairy black hole

2) Is this the end of the process?

In *theory* no; they are still afflicted by superradiant instabilities of higher  $m$  modes, because they have ergo-regions [CH and Radu PRD89\(2014\)124018](#)

higher  $m$  superradiance instability



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higher  $m$  superradiance instability

Kerr  $\xrightarrow{\Delta t}$  (astrophysical time scale) Hairy black hole  $\xrightarrow{> 1000\Delta t}$  ???  
(astrophysical time scale at highest efficiency, but cosmological or beyond off highest efficiency)

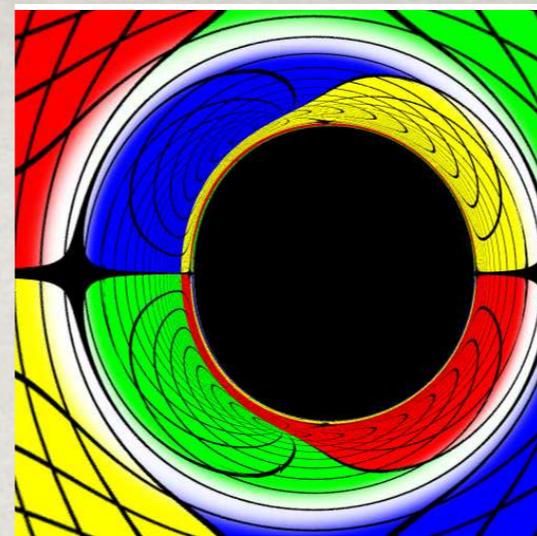
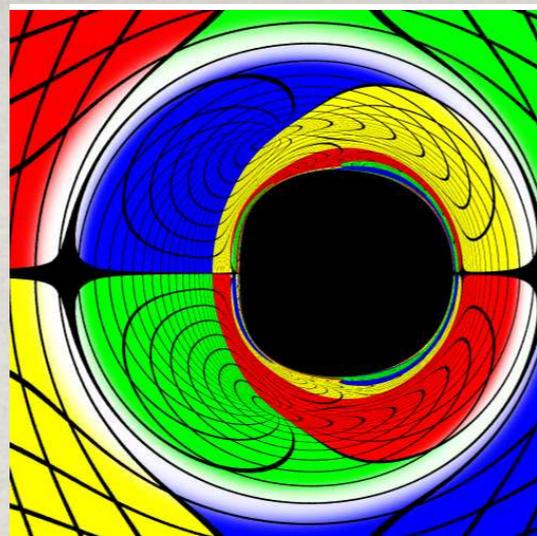
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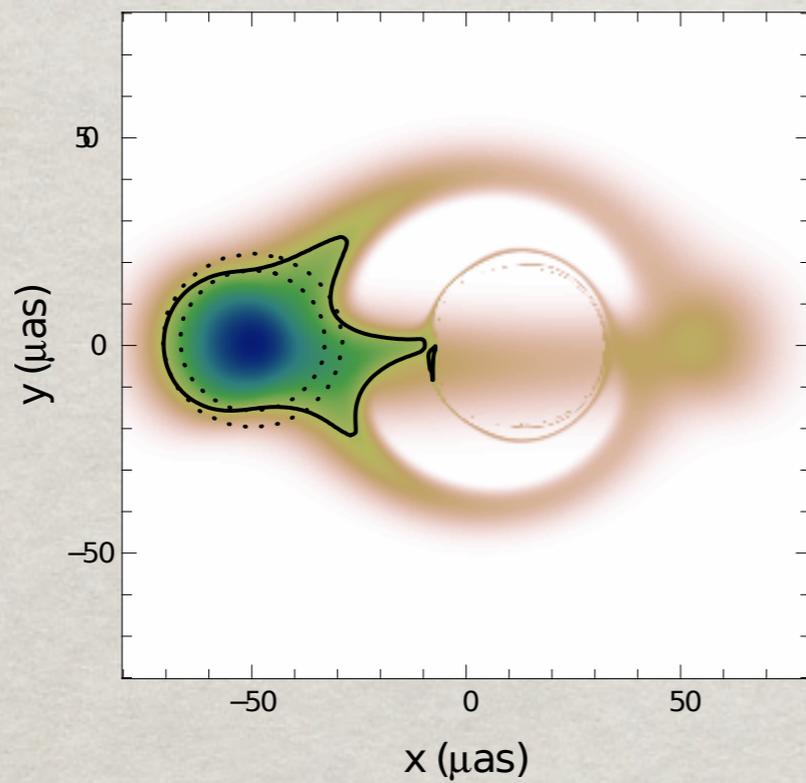
In *practice* it can be: **effective stability**

[Degollado, CH, Radu, 1802.07266](#)

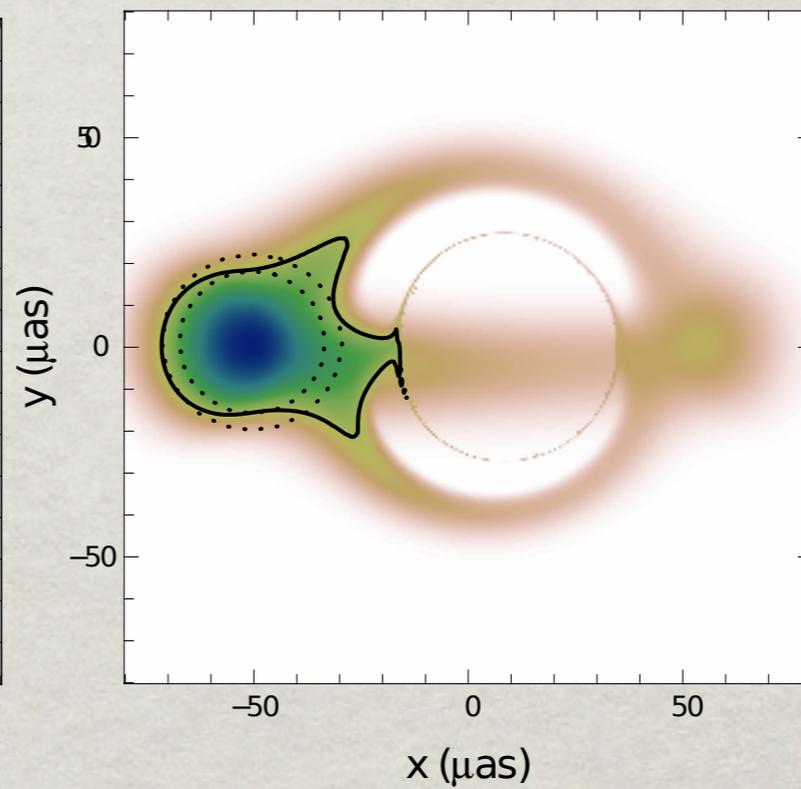
“Academic  
Sky”



KBHSH configuration II



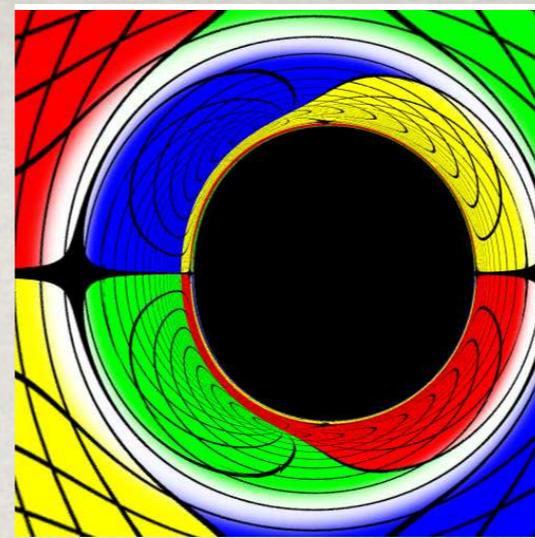
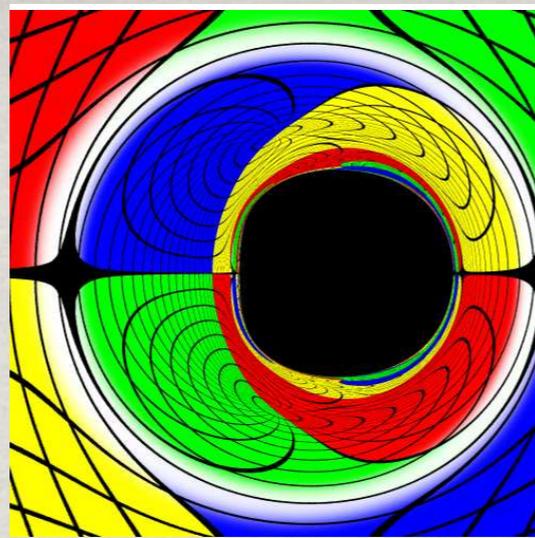
Kerr SP configuration II



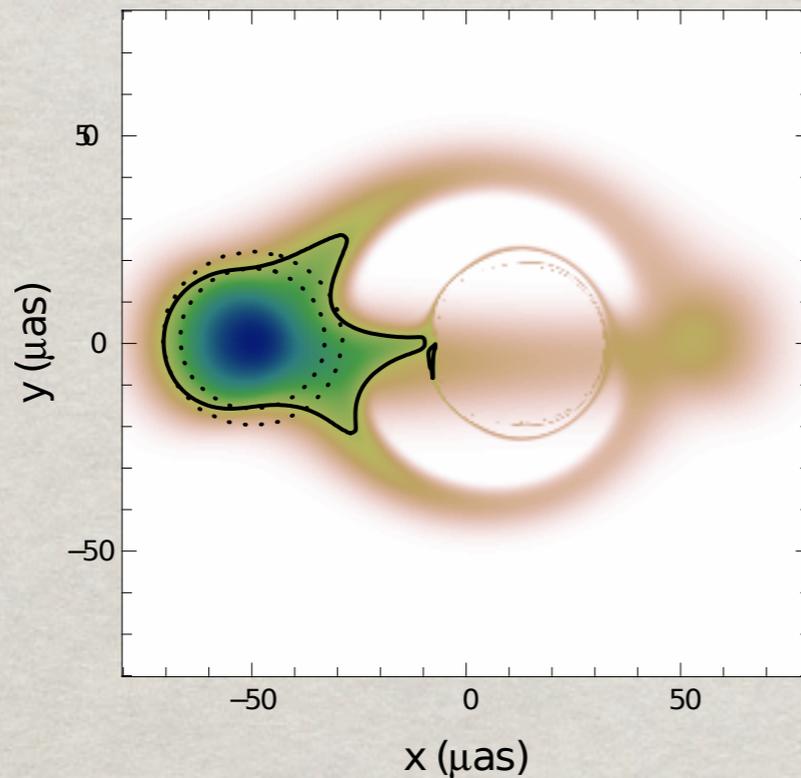
Differences remain in an astrophysically more realistic setup

Vincent, Gourgoulhon, CH, Radu, PRD94(2016)084045

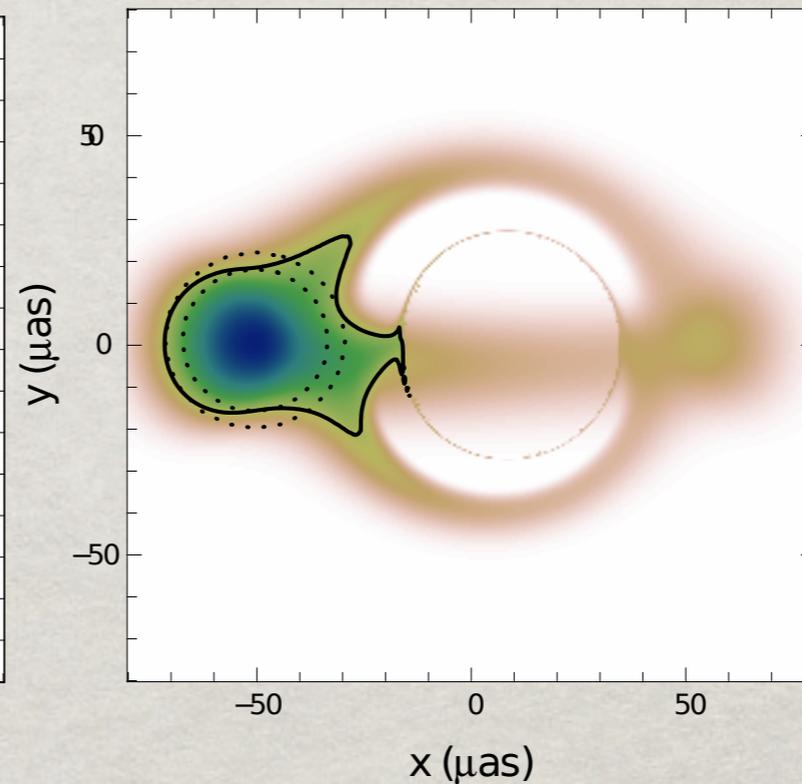
“Academic  
Sky”



KBHSH configuration II



Kerr SP configuration II



Differences remain in an astrophysically more realistic setup

Vincent, Gourgoulhon, CH, Radu, PRD94(2016)084045

Similar story for other observables such as the:

- iron  $K\alpha$ -line in the reflexion spectrum Ni, Zhou, Cardenas-Avendano, Bambi, CH, Radu, JCAP1610(2016)003
- QPOs Franchini, Pani, Maselli, Gualtieri, CH, Radu, Ferrari, PRD95(2017)124025

## a) In General Relativity

1) Appear in a well motivated and consistent physical model;

Kerr black holes with synchronised hair: General Relativity minimally coupled to massive bosonic fields

Check  
list!

2) Have a dynamical formation mechanism;

Kerr black holes with synchronised hair: superradiance instability of Kerr

3) Be (sufficiently) stable.

Kerr black holes with synchronised hair: effective stability against superradiance in some range of masses and couplings

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### Issues:

- What is the ultralight scalar/vector field?
- Interaction with astrophysical environment/accretion ?
  - Other instabilities ?

# Kerr black holes with synchronised bosonic hair

other references:

IJMPD23(2014)1442014	PRD89(2014)12; 124018	PLB739(2014)1	PRD90(2014)10, 104024	PLB739(2014)302
IJMPD24(2015)1542014	PLB748(2015)30	PLB752(2016)291	PRD92(2015)084059	PRL116(2016)141101
PLB760 (2016) 279-287	PRD94 (2016)084045	JCAP1607(2016)049	PRD94(2016)044061	PLB761 (2016) 234
JCAP1610(2016)003	PRD94(2016)104023	CQG34(2017)165001	PRD95(2017)124025	JCAP1708(2017)014
PRD95(2017)104028	PRD95(2017)104035	PLB773(2017)129	PRL119(2017)261101	JHEP1711(2017)037

with

C. Bambi, C. Benone, Y. Brihaye, R. Brito, A. Cardenas-Avendano, Z. Cao, V. Cardoso, L. C. Crispino, P. Cunha, J. C. Degollado, J. F. M. Delgado, , V. Ferrari, J. A. Font, N. Franchini, E. Gourgoulhon, J. Grover, L. Gualtieri, J. Kunz, A. Maselli, P. J. Montero, Y. Ni, P. Pani, H. Rúnarsson, N. Sanchis-Gual, T. Shen, B. Subagyo, F. Vincent, A. Wittig, M. Zhou

# Kerr black holes with synchronised bosonic hair

other references:

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Jorge Delgado's talk on the horizon geometry

João Oliveira's talk on virial identities

## b) Beyond General Relativity

Many models

One illustrative example: Einstein-dilaton-Gauss-Bonnet  
(arises in String Theory, second order equations of motion, etc...)

$$S = \frac{1}{16\pi} \int d^4x \sqrt{-g} \left[ R - \frac{1}{2} (\partial_\mu \phi)^2 + \alpha e^{-\gamma \phi} R_{\text{GB}}^2 \right],$$

$$R_{\text{GB}}^2 = R_{\mu\nu\rho\sigma} R^{\mu\nu\rho\sigma} - 4R_{\mu\nu} R^{\mu\nu} + R^2$$

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Schwarzschild/Kerr not solutions - new black holes which are stable in some regime, P. Kanti, N. E. Mavromatos, J. Rizos, K. Tamvakis and E. Winstanley, *Phys. Rev. D* 54 (1996) 5049; *Phys. Rev. D* 57 (1998) 6255; P. Kanti, B. Kleihaus and J. Kunz, *Phys. Rev. Lett.* 107 (2011) 271101

New qualitative features (minimal black hole size);

Various interesting cousin models changing the scalar/curvature coupling

Sotiriou and Zhou, *Phys. Rev. D* 90 (2014) 124063

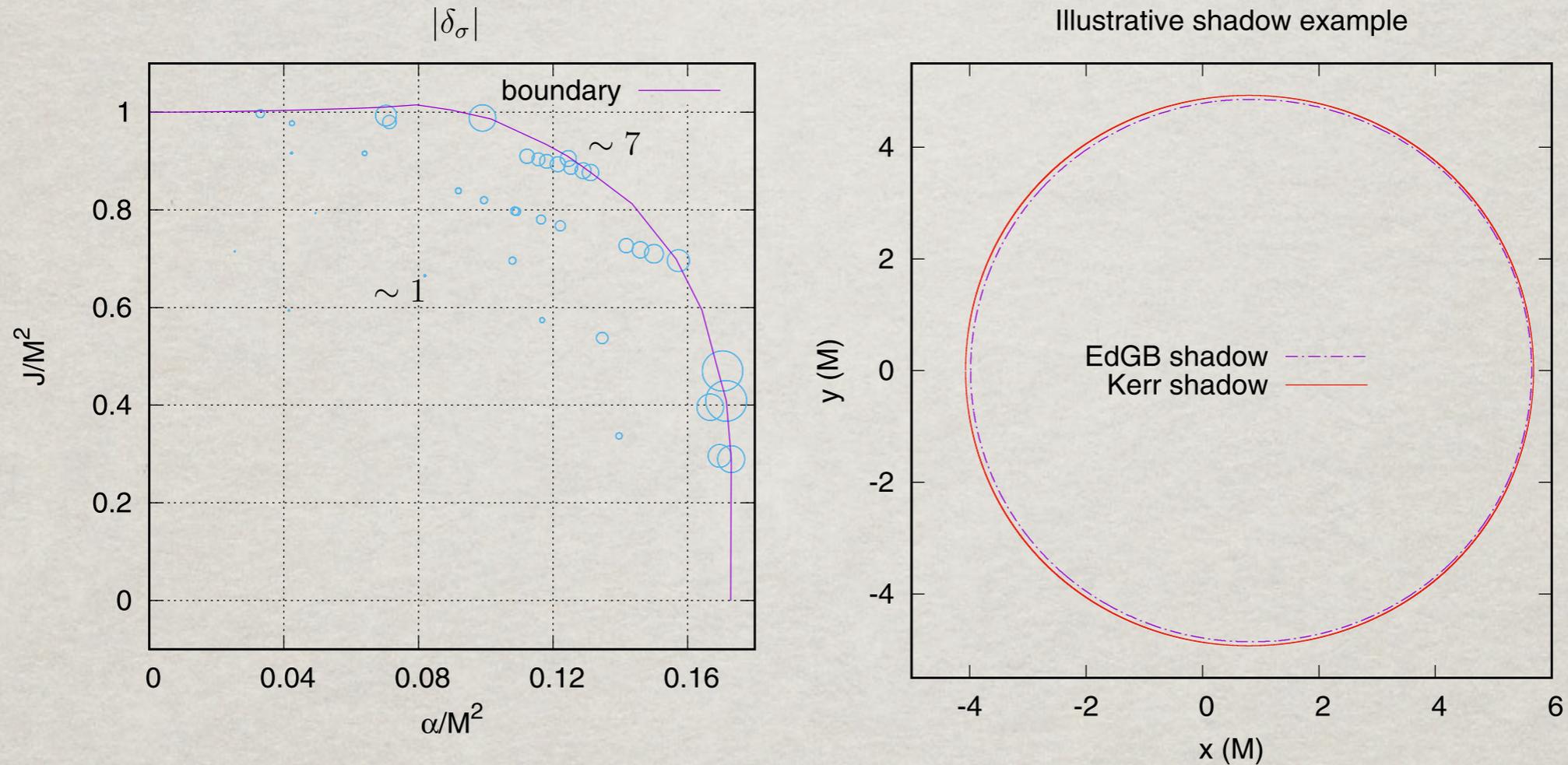
Silva, Sakstein, Gualtieri, Sotiriou, Berti, arXiv:1711.02080 [gr-qc];

Dynamical formation

Benkel, Sotiriou and Witek, *Phys. Rev. D* 94 (2016) 121503

## Phenomenology:

No large deviations from Kerr occur; e.g. shadows



**Fig. 4.** (Left) Representation of  $|\delta_\sigma|$  for EdGB solutions with  $\gamma = 1$ , in a  $\alpha/M^2$  vs.  $J/M^2$  diagram. Each circle radius is proportional to the quantity represented, with some values also included for reference. All the values of  $\delta_\sigma$  are negative. (Right) Depiction of the shadow edge of a EdGB BH with  $\gamma = 1$  and  $(\alpha/M^2, J/M^2) \simeq (0.172, 0.41)$ , yielding  $\bar{r} \simeq 4.85$ ,  $\sigma = 0.3$ ,  $x_C = 0.84$ ; the radial deviation  $\delta_r$  with respect to the comparable Kerr case is  $\simeq -1.35\%$ . The observer is at a perimetral radius  $15M$ .

The case of Einstein-dilaton-Gauss-Bonnet:  
the largest shadow deviation is (in the average radius) only  $\sim$  few %

Cunha et. al , PLB (2017)

Same for  $K\alpha$  line

Zhang, Zhou, Bambi, Kleihaus, Kunz and Radu, Phys. Rev. D 95 (2017) 104043

## **b) Beyond General Relativity**

## b) Beyond General Relativity

1) Appear in a well motivated and consistent physical model;

Einstein-dilaton-Gauss-Bonnet (or variations thereof)

2) Have a dynamical formation mechanism;

Gravitational collapse or scalarisation

3) Be (sufficiently) stable.

Some solutions are stable

Check  
list!

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Some solutions are stable

Check  
list!

### Issues:

- Why stop at quadratic curvature?
  - Why a certain coupling?
- There are effective violations of energy conditions. Is it an issue?

### **3) Beyond black holes**

## Black holes have a horizon and (abiding energy conditions) a curvature singularity: issues

To avoid this difficulties, models of horizonless compact objects (black hole mimickers) have been considered:

- a) “geons”, realized by Boson stars ([Schunck, Mielke, CQG 20 \(2003\) R301](#)) and Proca stars ([Brito, Cardoso, CH, Radu, PLB752 \(2016\) 291](#)); can form dynamically ([Seidel, Suen, PRL 72 \(1994\) 2516](#)); Perturbatively stable [Gleiser and Watkins, NPB 319 \(1989\) 733](#); [Lee and Pang, NPB 315 \(1989\) 477](#) ; Can be studied dynamically in binaries ([Liebling and Palenzuela LRR 20 \(2017\) 5](#))
- b) wormholes
- c) gravastars ([Mazur and Mottola, gr-qc/0109035](#))
- d) fuzzballs ([Mathur, Fortsch. Phys. 53 \(2005\) 793](#))
- e) ...

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b) wormholes

c) gravastars ([Mazur and Mottola, gr-qc/0109035](#))

d) fuzzballs ([Mathur, Fortsch. Phys. 53 \(2005\) 793](#))

e) ...

- To be able to mimic (up to a fine structure) the GW ringdown the object must be ultracompact, i.e. have a light ring [Cardoso, Franzin and Pani, PRL 116 \(2016\) 171101](#)

- Possible issue: for ultracompact objects resulting from a smooth, incomplete gravitational collapse, light rings come in pairs and one is stable [Cunha, Berti, CH, PRL 119 \(2017\) 251102](#)

### **3) Beyond black holes**

# 3) Beyond black holes

## Check list:

1) Appear in a well motivated and consistent physical model;

*Boson stars: General Relativity minimally coupled to massive bosonic fields*

Check  
list!

2) Have a dynamical formation mechanism;

*Gravitational cooling*

3) Be (sufficiently) stable.

*Some solutions are stable*

# 3) Beyond black holes

## Check list:

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Check  
list!

2) Have a dynamical formation mechanism;

*Gravitational cooling*

3) Be (sufficiently) stable.

*Some solutions are stable*

## Issues:

- What is the scalar field?
- No known dynamical formation mechanism for rotating boson stars;
  - Interaction with astrophysical environment/accretion ?
  - Are there perturbatively stable boson stars with light rings?

## **4) Outlook**

## Concluding remark:

All these models have caveats, but they illustrate that there exist fairly reasonable theoretical possibilities (albeit with admittedly exotic physics) of alternative models to the Kerr paradigm.

High risk, high gain endeavour: producing detailed phenomenology will constrain the model and the corresponding exotic physics or, in the best case scenario, provide a smoking gun to this new physics.

Testing the Kerr hypothesis by looking for alternative models represents scientific open mindedness.

Muchas gracias  
por su atencion!

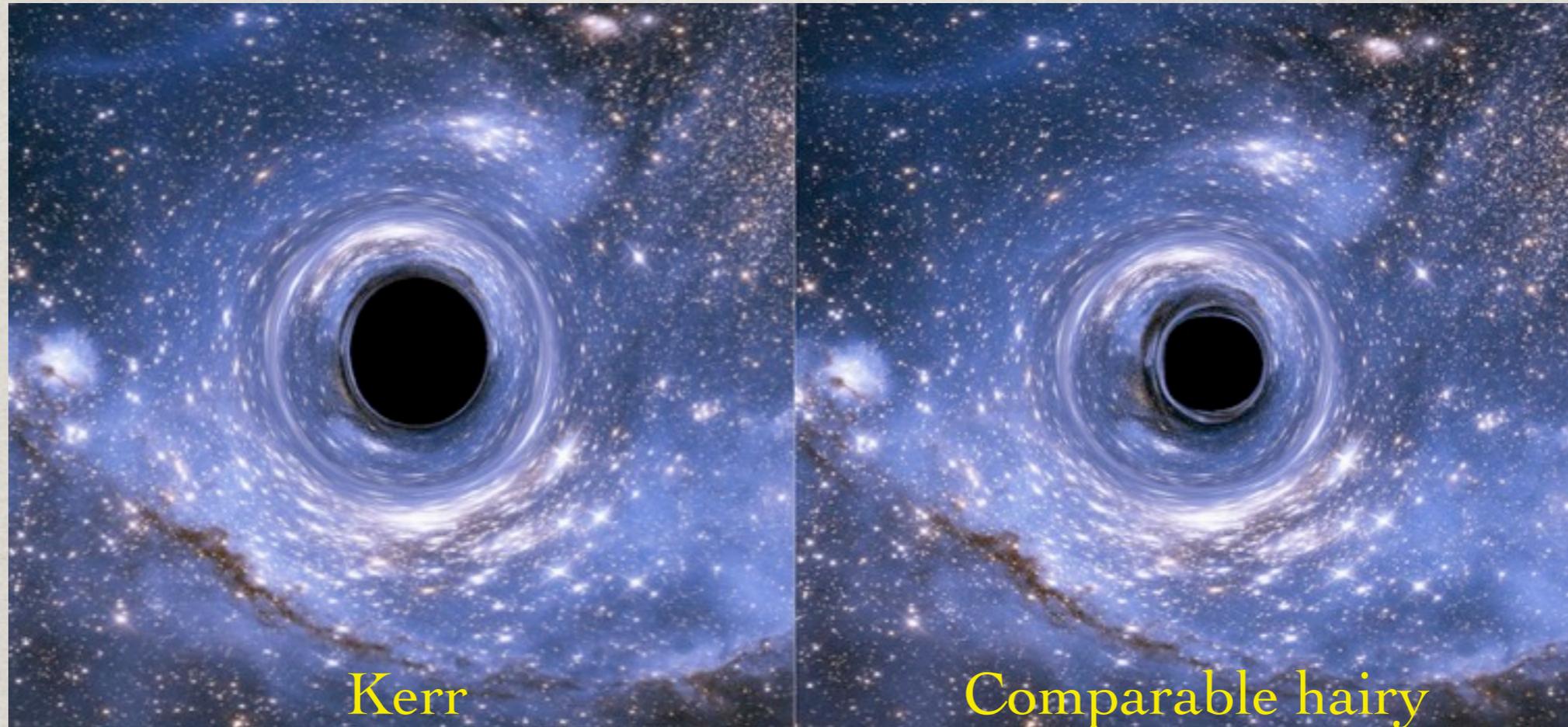


Image:  
P. Cunha

Thank you for Your  
Attention!